## Electronic Total Stations Are Levels Too

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Precise Trigonometric Leveling Using Modern Total Station Instruments

## Trigonometric Leveling



## Trigonometric Leveling Target



Side View

## Trig-Target Views At Various Distances



## Trigonometric Leveling Level Ground



## Observation Procedure

Pointings - 2 Sets of D\&R ZA $\quad$ What Gets Recorded?
1 Direct on Backsite
2 Swing Alidade
3 Direct on Foresite
4 Plunge Scope
5 Reverse on Foresite
6 Swing Alidade
7 Reverse on Backsite
That completes one set of
Direct and Reverse Pointings
8 Re-point on Backsite in Reverse
9 Swing Alidade
10 Reverse on Foresite
11 Plunge Scope
12 Direct on Foresight
13 Swing Alidade
14 Direct on Backsite

Vertical Distances to the millimeter or tenth of a millimeter.
Be sure to record the algebraic sign!!!
Slope Distances to the nearest decimeter just to keep track of the distance traveled.

Make sure that all the necessary corrections are being applied!!!

Temperature
Pressure
PPM
EDM Constant
Reflector Constant
Curvature and Refraction

A Data Collector with a Trig Leveling Routine would be great!!!!

## Trigonometric Leveling <br> Leveling Up Hill



## Trigonometric Leveling Leveling Down Hill



## Trigonometric Leveling

Leveling Down and Up Hill

Backsight
Difference In Elevation
$=+1.115 \mathrm{~m}$


## Trigonometric Leveling

Leveling Up and Down Hill


## Conventional Differential Leveling

## Balanced Setup

Consistent collimation error CANCELS in a BALANCED setup since the BACKSIGHT distance is equal to the FORESIGHT distance.


## Conventional Differential Leveling

## Imbalanced Setup



## Trigonometric Leveling Imbalanced Setup



Collimation ERROR CANCELS in a BALANCED or IMBALANCED SETUP in TRIGONOMETRIC LEVELING

## Conventional Differential Leveling

## Refraction Effects

Refraction error, r, DOES NOT CANCEL on SLOPING terrain since $r_{B}$ is NOT EQUAL to $r_{F}$, even if $S_{B}$ is EQUAL TO $S_{F}$


## Trigonometric Leveling

Refraction Effects


## How Far?

That primarily depends on the precision of the vertical circle.


## 1mm EDM and 0.5 Second Total Station

## Zenith Angle

|  |  | 89 | 88 | 87 | 86 | 85 | 84 | 83 | 82 | 81 | 80 | 79 | 78 | 77 | 76 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10 | 0.03 | 0.04 | 0.06 | 0.07 | 09 | 0.11 | 0. | 0.14 | 0.16 | 0.18 | 0.19 | 1 | 23 | 0.24 | 0.26 |
|  | 20 | 0.05 | 0.06 | 0.07 | 0.08 | 0.10 | 0.12 | 0.13 | 0.15 | 0.16 | 0.18 | 0.20 | 0.21 | 0.23 | 0.25 | 6 |
|  | 30 | 0.07 | 0.08 | 0.09 | 0.10 | 0.11 | 0.13 | 0.14 | 0.16 | 0.17 | 0.19 | 0.20 | 0.22 | 0.24 | 0.25 | . 27 |
|  | 40 | 0.10 | 0.10 | 0.11 | 0.12 | 0.13 | 0.14 | 0.16 | 0.17 | 0.18 | 0.20 | 0.21 | 0.23 | 0.24 | . 26 | 28 |
|  | 50 | 0.12 | 0.13 | 13 | 0 | 15 | 0.16 | 0. | 0.18 | 0.20 | 0.21 | 0.22 | 0.24 | 0.25 | . 27 | 28 |
|  | 60 | 0.15 | 0.15 | 0.15 | 0.16 | 0.17 | 0.18 | 0.19 | 0.20 | 0.21 | 0.23 | 0.24 | 0.25 | 0.27 | 0.28 | 29 |
|  | 70 | 0.17 | 0.17 | 0.18 | 0.18 | 0.19 | 0.20 | 0.21 | 0.22 | 0.23 | 0.24 | 0.25 | 0.27 | 0.28 | 0.29 | 31 |
|  | 80 | 0.19 | 0.20 | 0.20 | 0.21 | 0.21 | 0.22 | 0.23 | 0.24 | 0.25 | 0.26 | 0.27 | 0.28 | 0.29 | 0.31 | 32 |
|  | 90 | 0.22 | 0.22 | 0.22 | 0.23 | 0.23 | 0.24 | 0.25 | 0.26 | 0.27 | 0.28 | 0.29 | 0.30 | 0.3 | 0.32 | . 33 |
|  | 100 | 0.24 | 0.24 | 0.25 | 0.25 | 0.26 | 0.26 | 0.27 | 0.28 | 0.29 | 0.30 | 0.31 | 0.32 | 0.33 | 0.34 | . 3 |
|  | 110 | 0.27 | 0.27 | 0.27 | 0.27 | 0.28 | 0.29 | 0.29 | 0.30 | 0.31 | 0.31 | 0.32 | 0.33 | 0.34 | 0.35 | . 7 |
|  | 120 | 0.29 | 0.29 | 0.30 | 0.30 | 0.30 | 0.3 | 0.31 | 0.32 | 0.33 | 0.33 | 0.34 | 0.35 | 0.36 | 0.37 | 38 |
|  | 130 | 0.32 | 0.32 | 0.32 | 0.32 | 0.33 | 0.33 | 0.34 | 0.34 | 0.35 | 0.36 | 0.36 | 0.37 | . 38 | 0.39 | 40 |
|  | 140 | 0.34 | 0.34 | 0.34 | 0.35 | 0.35 | 0.35 | 0.36 | 0.36 | 0.37 | 0.38 | 0.38 | 0.39 | 0.40 | 0.41 | 42 |
|  | 150 | 0.36 | 0.37 | 0.37 | 0.37 | 0.37 | 0.38 | 0.38 | 0.39 | 0.39 | 0.40 | 0.40 | 0.41 | 0.42 | 0.43 | 44 |
|  | 160 | 0.39 | 0.39 | 0.39 | 0.39 | 0.40 | 0.40 | 0.40 | 0.41 | 0.41 | 0.42 | 0.43 | 0.43 | 0.44 | 0.45 | 46 |
|  | 170 | 0.41 | 0.41 | 0.41 | 0.42 | 0.42 | 0.42 | 0.43 | 0.43 | 0.44 | 0.44 | 0.45 | 0.45 | 0.46 | 0.47 | 0.47 |
|  | 180 | 0.44 | 0.44 | 0.44 | 0.44 | 0.44 | 0.45 | 0.45 | 0.45 | 0.46 | 0.46 | 0.47 | 0.47 | 0.48 | 0.49 | . 49 |
|  | 190 | 0.46 | 0.46 | 0.46 | 0.46 | 0.47 | 0.47 | 0.47 | 0.48 | 0.48 | 0.49 | 0.49 | 0.50 | 0.50 | 0.51 | 1 |
|  | 200 | 0.49 | 0. | 0. | 0. | 0. | 0. | 0 | 0 | 0.50 | 0.51 |  | 0.52 |  | 5 |  |

## Expected Accuracy (mm)

## 1mm EDM and 1.0 Second Total Station

Zenith Angle

|  | 89 | 88 | 87 | 86 | 85 | 84 | 83 | 82 | 81 | 80 | 79 | 78 | 77 | 76 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 0.05 | 0.06 | 0.07 | 0.08 | 0.10 | 0.12 | 0.13 | 0.15 | 0.16 | 0.18 | 0.20 | 0.21 | 0.23 | 25 | 26 |
| 20 | 0.10 | 0.10 | 0.11 | 0.12 | 13 | 0.14 | 0.16 | 7 | 0.18 | 0.20 | 1 | 2 | 4 |  | 0.28 |
| 30 | 0. | 15 | 0.15 | 0 | 17 | 0. | 0. | 0.20 | 0. | 0.23 | 0.24 | 0.25 | 27 | 28 | 0.29 |
| 40 | 0.19 | 0.20 | 0.20 | 0.21 | 0.21 | 0.22 | 0.23 | 0.24 | 0.25 | 0.26 | 0.27 | 0.28 | 0.29 | 0.31 | . 32 |
| 50 | 0.24 | 0.24 | 0.25 | 0.25 | 0.26 | 0.26 | 0.27 | 0.28 | 0.29 | 0.30 | 0.31 | 0.32 | 0.33 | 0.34 | . 35 |
| 60 | 0.29 | 0.29 | 0. | 0.30 | 0.30 | 0. | 0.31 | 0.32 | 0.33 | 0.33 | 0.34 | 0.35 | 36 | 37 | . 38 |
| 70 | 0.3 | 0.3 | 0.34 | 0.35 | 0.35 | 0.3 | 0.36 | 0.36 | 0.37 | 0.38 | 0. | 0.39 | 0.40 | 0.41 | 42 |
| 80 | 0.39 | 0.39 | 0. | 0.39 | 0.40 | 0.40 | 0.40 | 0. | 0.41 | 0.42 | 0.43 | 0.43 | 0.44 | 45 | 46 |
| 90 | 0.44 | 0.44 | 0. | 0.44 | 0.44 | 0.45 | 0.45 | 0.45 | 0.46 | 0.46 | 0.47 | 0.47 | 0.48 | 0.49 | 49 |
| 100 | 0.49 | 0.49 | 0. | 0.49 | 0.49 | 0.49 | 0.50 | 0. | 0.50 | 0.51 | 0. | 0.52 | 0.52 | 0.53 | . 54 |
| O0 110 | 0.53 | 0.53 | 0.5 | 0.54 | 0.54 | 0.54 | 0.54 | 0.55 | 0.55 | 0.55 | 0.56 | 0.56 | 57 | 0.57 | . 58 |
| $\sim 120$ | 0.58 | 0.58 | 0.58 | 0.58 | 0.59 | 0.59 | 0.59 | 0.59 | 0.60 | 0.60 | 0.60 | 0.61 | 0.61 | 0.61 | 0. 62 |
| 130 | 0.63 | 0.63 | 0 | 0.63 | 0.63 | 0.6 | 0.64 | 0.64 | 0.6 | 0.64 | 0.65 | 0.65 | 0.65 | 6 | 66 |
| 140 | 0.68 | 0.68 | 0.6 | 0.6 | 0.68 | 0.6 | 0.68 | 0. | 0.6 | 0.69 | 0. | 0.70 | 0.70 | 0.70 | 0.70 |
| 150 | 0.73 | 0.73 | 0.73 | 0.73 | 0.73 | 0.73 | 0.73 | 0.73 | 0.74 | 0.74 | 0.74 | 0.74 | 74 | 75 | 0.75 |
| 160 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.78 | 0.79 | 0.79 | 0.79 | 0.79 |
| 170 | 0.82 | 0.82 | 0.82 | 0.83 | 0.83 | 0.83 | 0.83 | 0.83 | 0.83 | 0.83 | 0.83 | 0.83 | 0.83 | 0.84 | . 84 |
| 180 | 0.87 | 0.87 | 0.87 | 0.87 | 0.87 | 0.87 | 0.87 | 0.88 | 0.88 | 0.88 | 0.88 | 0.88 | 0.88 | 0.88 | . 88 |
| 190 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.92 | 0.93 | 0.93 | 0.93 |
| 200 | 0.97 | 0.97 | 0.9 | 0.97 | 0.97 | 0.97 | 0.97 | 0.97 | 0.9 | 0.97 | 0. | 0.97 | 0.97 | 0.97 |  |

Expected Accuracy (mm)

## 2mm EDM and 3.0 Second Total Station

## Zenith Angle

|  |  | 89 | 88 | 87 | 86 | 85 | 84 | 83 | 82 | 81 | 80 | 79 | 78 | 77 | 76 | 75 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.1 | 0.1 | 0.1 | 0.20 | 0.23 | 0.25 | 0. | 0. | 0. | 0.38 | 0.41 | 0.44 | 0.47 | 0.50 | 0.54 |
|  | 20 | 0.2 | 0.30 | 0.31 | 0.32 | 0.34 | 0.36 | 0.3 | 0.4 | 0.42 | 0.45 | 0.48 | 50 | 0.53 | 0.56 | 0.59 |
|  | 30 | 0. | 0.4 | 0.45 | 0.46 | 0.47 | 0.48 | 0.50 | 0. | 0.53 | 0.55 | 0.57 | 0.60 | 0.6 | 0.64 | 0.67 |
|  | 40 | 0.5 | 0.5 | 0.5 | 0.60 | 0.61 | 0.62 | 0.63 | 0.6 | 0.65 | 0.67 | 0.69 | 0.70 | 0.7 | 0.74 | 0.76 |
|  | 50 | 0.73 | 0.7 | 0.73 | 0.74 | . 75 | 0.75 | 0.76 | 0.77 | 0.78 | 0.80 | 0.81 | 0.82 | 0.84 | 0.86 | 0.87 |
|  | 60 | 0.87 | 0.87 | 0.88 | 0.88 | 0.89 | 0.89 | 0.90 | 0.91 | 0.92 | 0.93 | 0.94 | 0.95 | 0.96 | 0.98 | 0.99 |
|  | 70 | 1.02 | 1.02 | 1.02 | 1.03 | 1.03 | 1.03 | 1.04 | 1.05 | 1.05 | 1.06 | 1.07 | 1.08 | 1.09 | 1.10 |  |
|  | 80 | 1.16 | 1.16 | 1.17 | 1.17 | 1.17 | 1.18 | 1.18 | 1.19 | 1.19 | 1.20 | 1.20 | 1.21 | 1.22 | 1.23 | 1.24 |
|  | 90 | 1.31 | 1.31 | 1.31 | 1.31 | 1.32 | 1.32 | 1.32 | 1.33 | 1.33 | 1.34 | 34 | 35 | 1.35 | 1.36 | 1.37 |
|  | 100 | 1.45 | 1.46 | 1.46 | 1.46 | 1.46 | 1.46 | 1.46 | 1.47 | 1.47 | 1.47 | 1.48 | 1.48 | 1.49 | 1.49 | . 50 |
|  | 110 | 60 | 1.60 | 1.60 | 1.60 | 1.60 | 1.60 | 1.61 | 1.61 | 1.61 | 1.61 | 1.62 | 1.62 | 1.62 | 1.63 | 63 |
|  | 120 | 1.75 | 1.75 | 1.75 | 1.75 | 1.75 | 1.75 | 1.75 | 1.75 | 1.75 | 1.75 | 1.76 | 1.76 | 1.76 | 1.76 | 1.76 |
|  | 130 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.89 | 1.90 | 1.90 | 1.90 | 1.90 |
|  | 140 | 2.04 | 2.04 | 2.04 | 2.04 | 2.04 | 2.04 | 2.04 | 2.04 | 2.04 | 2.04 | 2.03 | 2.03 | 2.03 | 2.03 | . 03 |
|  | 150 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.18 | 2.17 | 2.17 | 2.17 | .17 |
|  | 160 | 2.33 | 2.33 | 2.33 | 2.33 | 2.32 | 2.32 | 2.32 | 2.32 | 2.32 | 2.32 | 2.32 | 2.31 | 2.31 | 2.31 | . 31 |
|  | 170 | 2.47 | 2.47 | 2.47 | 2.47 | 2.47 | 2.47 | 2.47 | 2.46 | 2.46 | 2.46 | 2.46 | 2.45 | 2.45 | 2.4 | . 44 |
|  | 180 | 2.62 | 2.62 | 2.62 | 2.62 | 2.61 | 2.61 | 2.61 | 2.61 | 2.60 | 2.60 | 2.60 | 2.59 | 2.59 | 2.59 | 58 |
|  | 190 | 2.76 | 2.76 | 2.76 | 2.76 | 2.76 | 2.76 | 2.75 | 2.75 | 2. | 2.74 | 2.74 | 2.73 | 2.73 | 2.72 |  |
|  | 200 | 2.91 | 2.91 |  |  |  | 2.90 |  |  |  |  |  |  |  |  |  |

## Expected Accuracy (mm)

