

Overview of TLS systems, overall processing and applications

Theory and Application of Laser Scanning

ISPRS Summer School 2007

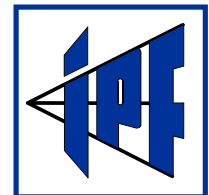
Ljubljana, Solvenia



Norbert Pfeifer

Institute of Photogrammetry and Remote Sensing

Vienna University of Technology, Austria

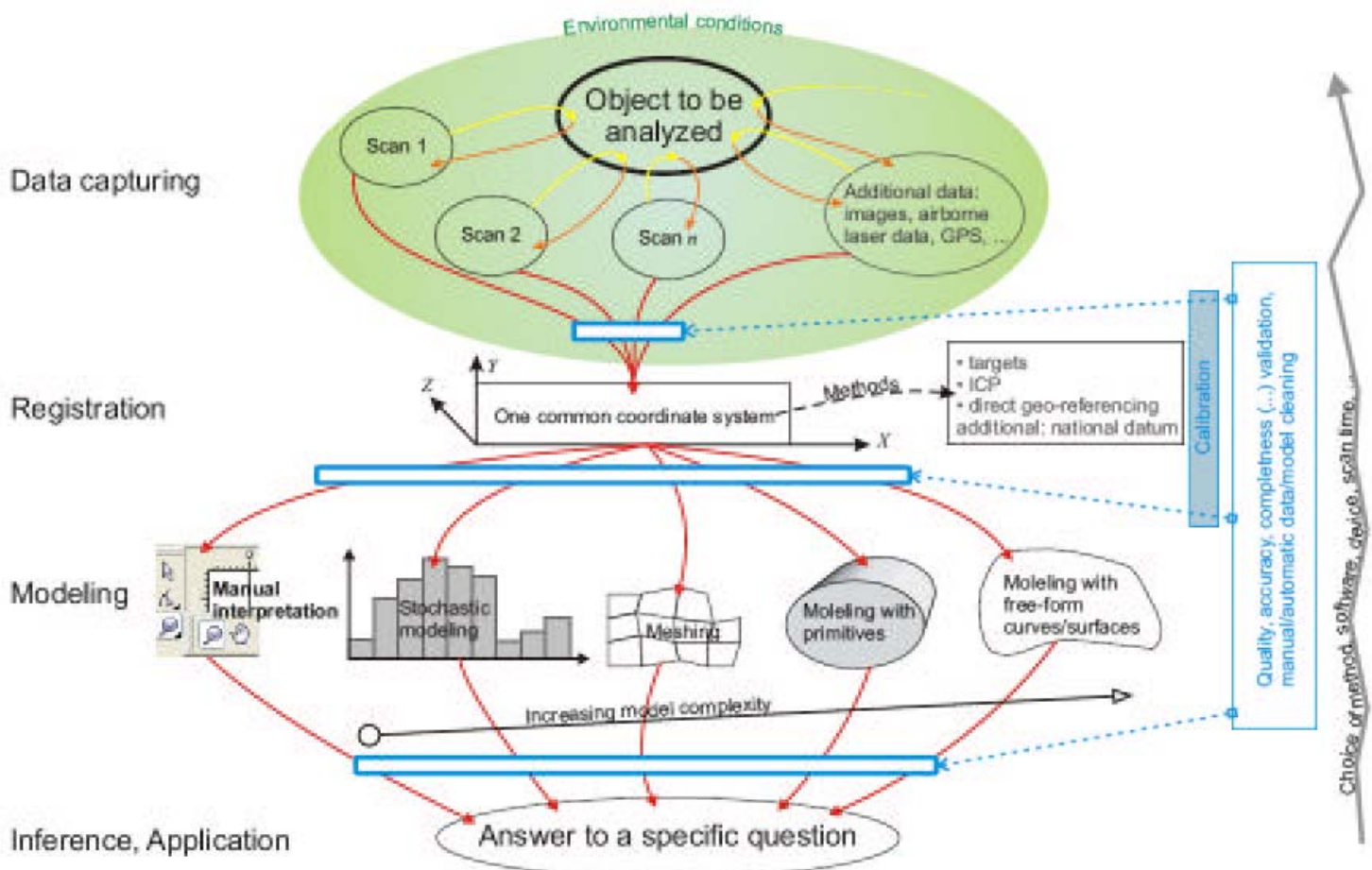


Lecture outline

- Definition: Laser Scanning
- Measurement principles
- Presentation of different instruments
- Comparison to other techniques
- Registration overview
- Modeling overview
- Application overview

N.B., material partly taken from

- Kraus, 2004. Photogrammetrie, 7th ed., Dümmler, Germany.
- Boehler, Marbs: 3D Scanning Instruments. CIPA WG6 Internat. Workshop, Scanning for Cultural Heritage Recording, Corfu, Greece, 2002.
- Websites of device producers: Riegl, Trimble, Hexagon, Optech



Competing Complementing Measurement Tools



mer Schol
ing 2007



© Boeing, Soenh, Leica, Riegl, Nikon,
Optech, Callidus, Rollei, Trimble,
Minolta



Definitions

- Definition: TLS
= Terrestrial Laser Scanning
data point of view
- TLS systems
= Terrestrial Laser Scanner
component point of view

Terrestrial Laser Scanning

Definition

Terrestrial Laser Scanning

- is a technique
- using laser light
- for measuring
- in a regular pattern
- directly
- 3D coordinates
- of points
- on surfaces
- from a terrestrial position

measurement errors

Photogrammetry
direct: 2D coordinates
compute: 3D coordinates

no corners, no edges
Tacheometry +
Photogrammetry:
corners and edges

ground, building, car, ...

synthetic Example - I

- measure polar coordinates φ , α , r (3D coordinates)

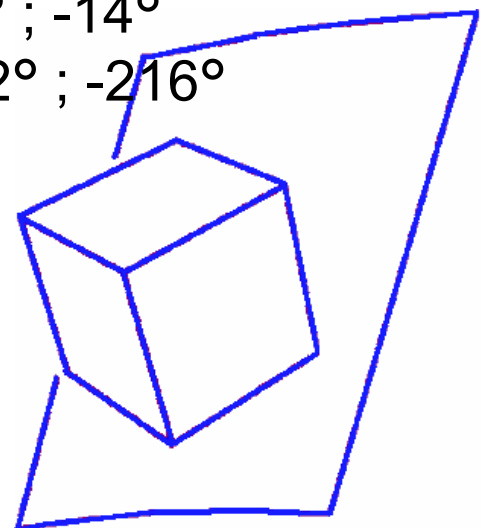
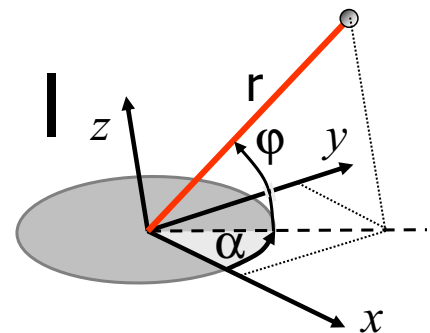
- regular pattern

$$\varphi_{i+1} - \varphi_i = 1^\circ \quad \varphi \text{ min ; max} = -30^\circ ; -14^\circ$$

$$\alpha_{j+1} - \alpha_j = 1^\circ \quad \alpha \text{ min ; max} = -232^\circ ; -216^\circ$$

- measure range r for all φ_i , α_j

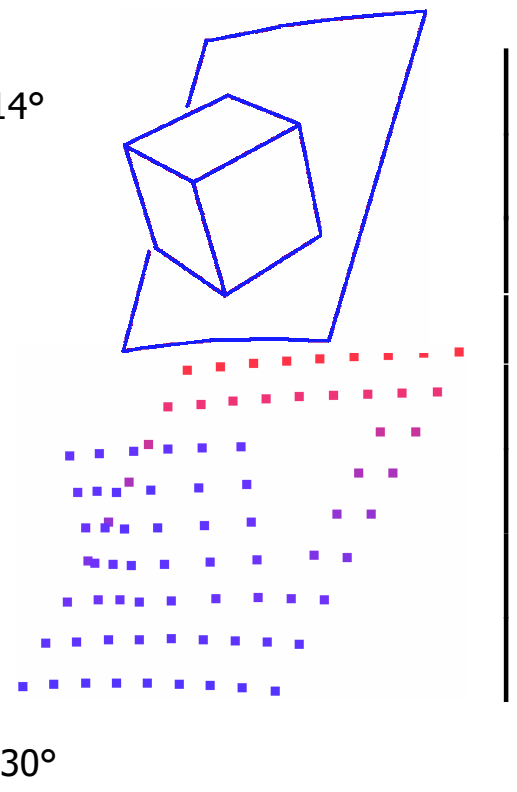
- object (surfaces) measured in this example:
cube and base plane



synthetic Example - I I

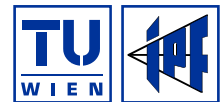
distance color coded
and written in meter

		horizontal angle									
		12,4	12,4	12,4	12,4	12,4	12,4	12,4	12,4	12,40	$\varphi = -14^\circ$
		10,9	10,9	10,9	10,9	10,9	10,9	10,9	10,9	10,88	
vertical angle		9,71	6,54	6,47	6,47	6,47	6,47	6,54	9,71	9,71	
		8,77	6,62	6,36	6,13	6,13	6,36	6,62	8,77	8,77	
		8,01	6,71	6,45	6,21	6,21	6,45	6,71	8,01	8,01	
		7,38	6,81	6,54	6,3	6,3	6,54	6,81	7,38	7,38	
		6,84	6,84	6,65	6,41	6,41	6,65	6,84	6,84	6,84	
		6,39	6,39	6,39	6,39	6,39	6,39	6,39	6,39	6,39	
		6,00	6,00	6,00	6,00	6,00	6,00	6,00	6,00	6,00	$\varphi = -30^\circ$

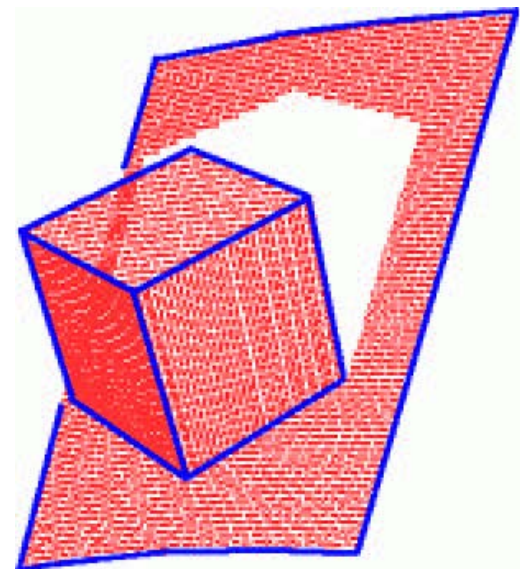
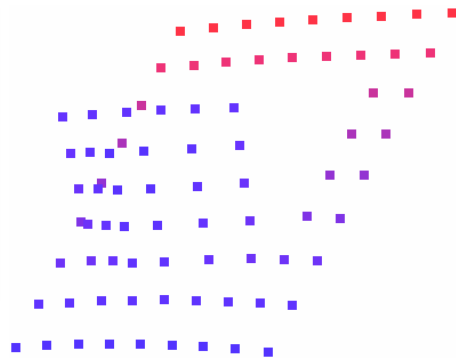
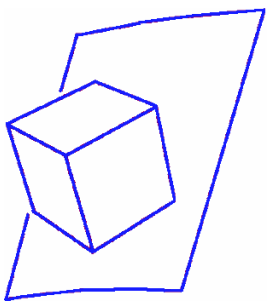


$\alpha = -216^\circ$

$\alpha = -232^\circ$



synthetic Example - I I I



Object low resolution scan
 high resolution scan

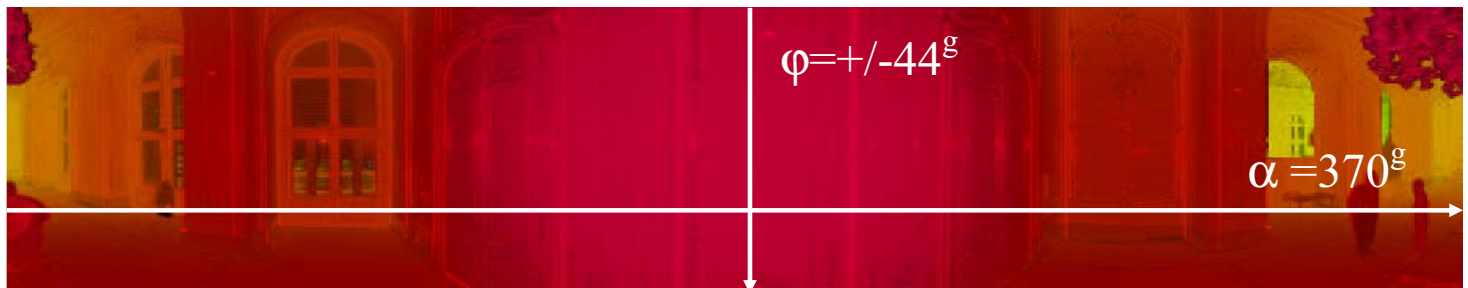
- Varying point density
- Shadows
- Edges *not* measured



real Example

Field of View (FoV)

- φ min ; max = -40° ; 40° $\varphi_{i+1} - \varphi_i = 0.25^\circ$
- α min ; max = 0° ; 333° $\alpha_{j+1} - \alpha_j = 0.25^\circ$
- r close ; far away = pink–red–orange–yellow–green
50cm – 10m
- 422,400 measurements of φ , α , r
- Measurement frequency: 2kHz (2000 measurements per second)
- Time for measurement: < 4 minutes



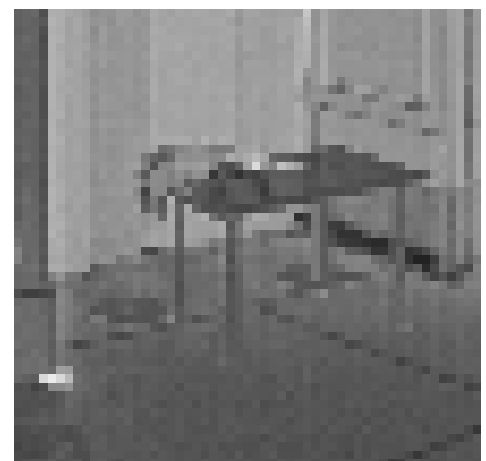
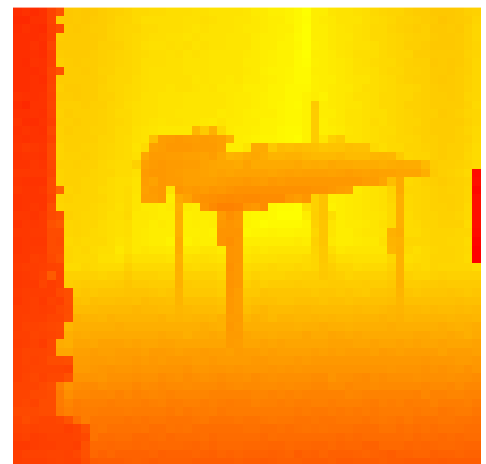
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real Example

Small detail from one scan

- Range image
regular φ , α – raster
- Point cloud in 3D
in Cartesian coordinate system
- Additional measurement
not only range to surface
but **also** *brightness* of surface



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improved Definition

Terrestrial Laser Scanning

Terrestrial Laser Scanning

- is a technique
- using laser light
- for measuring
- **with high speed**
- in a **dense** regular pattern
- directly
- 3D coordinates
- of points
- on surfaces
- **and surface brightness**
- from a terrestrial position

Terrestrial Laser Scanners

System components

- So far: data description from terrestrial laser scanning
- Now: How are the measurements performed?
- Concentration on φ , α , r (not brightness)

- Range r
pulse round trip – phase comparison – triangulation
- Laser beam angles φ , α
rotating mirrors – rotating instrument

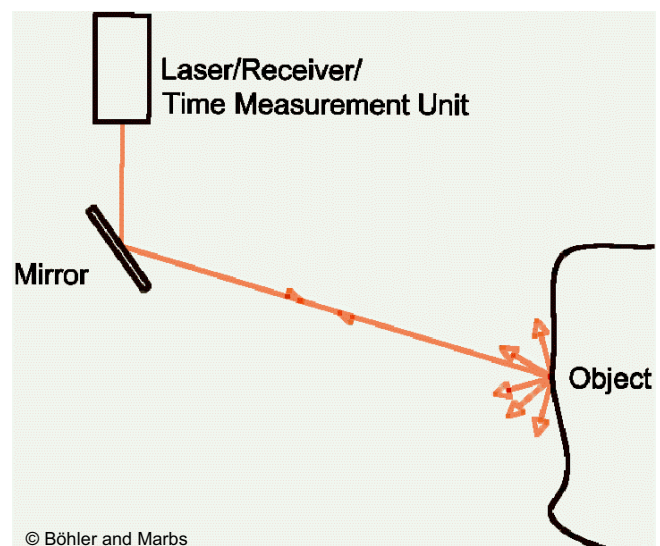
Measurement principles

- Distance measurement
 - Round trip time of a pulse
 - Phase comparison of a continuous wave
 - Triangulation
- & laser beam angle measurement

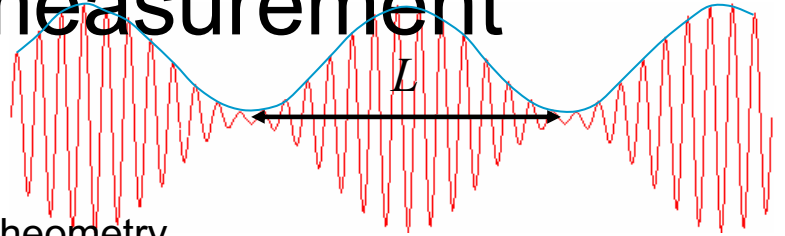
Distance measurement

Pulse round trip:

- measure time lapse between sent and received pulse
- 1cm = ns (nano-seconds)
- round trip time for 10m
between scanner and object = ns
- accuracy (almost) independent of distance
- suitable for longer ranges
(using higher pulse energies)
- increase accuracy by
averaging of multiple shots
- accuracy depends on strength
of backscattered signal:
object reflectivity + distance

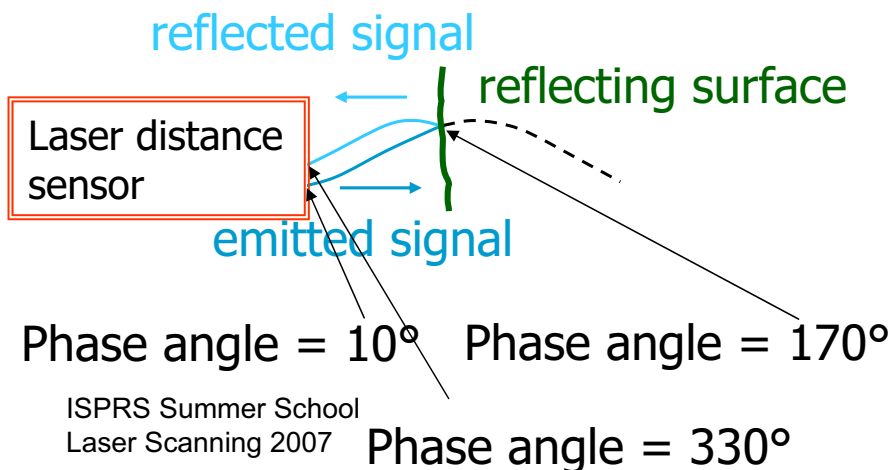


Distance measurement



Phase comparison:

- Similar to electronic distance measurement in tacheometry
- modulate laser light with harmonic signal (image: amplitude modulation)
- measure phase difference between emitted and received modulated signal



Example:

Phase difference =

$$= 330^\circ - 10^\circ = 320^\circ$$

$L = 100\text{m}$

Distance =

$$= 320^\circ / 360^\circ * L / 2 = 44.4\text{m}$$

Distance measurement

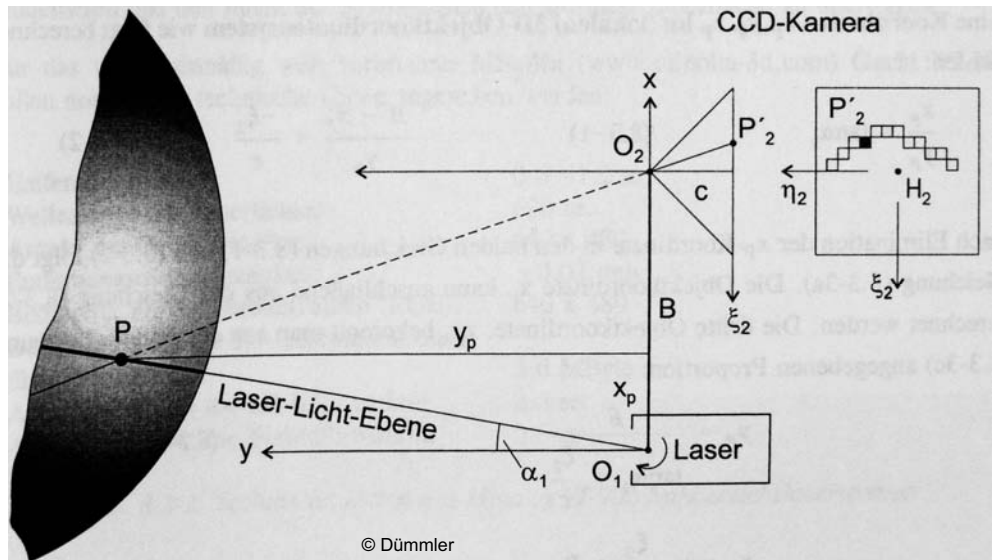
Phase comparison (2):

- uniqueness range = $\frac{1}{2}$ modulation wave length L
reflecting surfaces in distances d and $d + L/2$
return the same signal
- measure distances 'continuously' ... fast
- increase accuracy by
using shorter modulation wave lengths
- Use multiple modulation waves of different length
longest wave length defines uniqueness range
- accuracy depending on (shortest) modulation wave length,
but depending also on object reflectivity

Triangulation

Similar to photogrammetric normal case

- plane of (laser) light sweeps over object: angle $\alpha = \alpha(t)$
- light plane — object intersection mapped in digital image
- light plane — bundle of mapped curved points forward intersection
- for each plane (α) set of 3D points



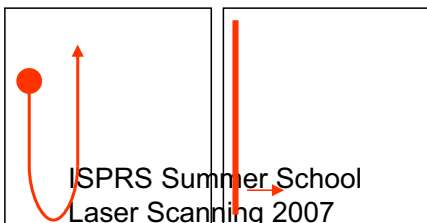
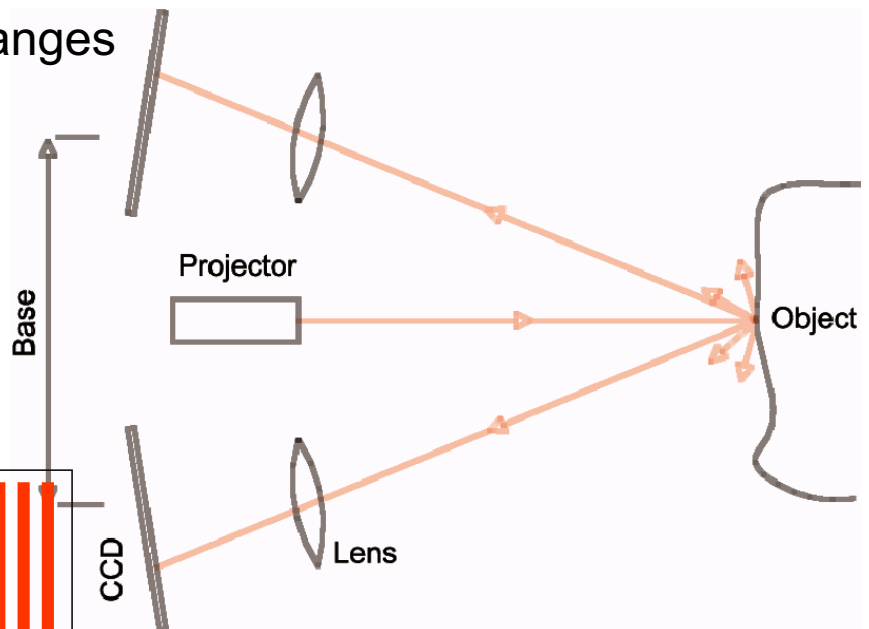
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Triangulation

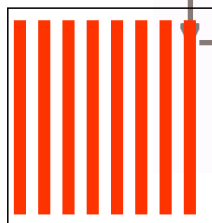
- accuracy depends on intersection quality base length vs. object distance
- accuracy decreases with distance²
- suitable for short ranges

Alternatives:

- use laser beam (i.e., no plane)
- use 2 cameras and one projector



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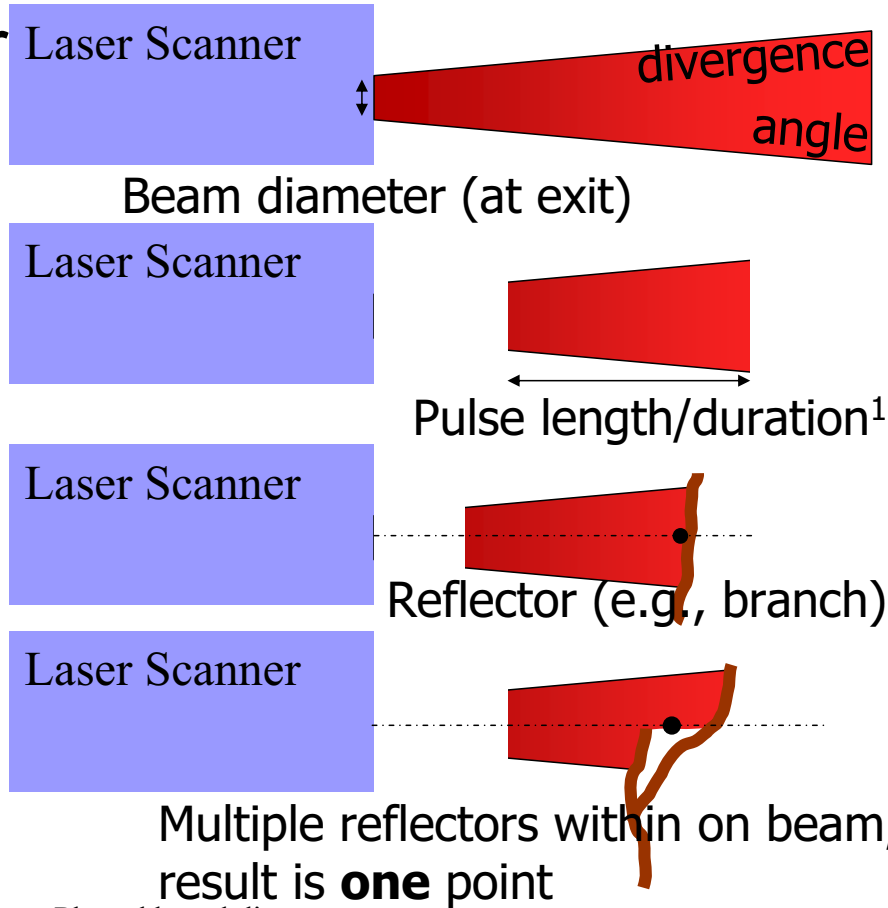


© Böhler and Marbs

Beam diameter and Pulse length

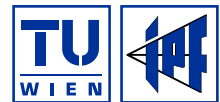
- Effect ...
... next slide

Pulse round trip time
scanners CAN
(theoretically) differentiate
first and last echo.



1: applies to pulse round trip time scanners. Phased based distance measurement uses a permanent signal.

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... Effect

on measurement: Phantom points²



2: phantom points are generated with pulse round trip time and phased based distance measurement scanners.

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Example 1

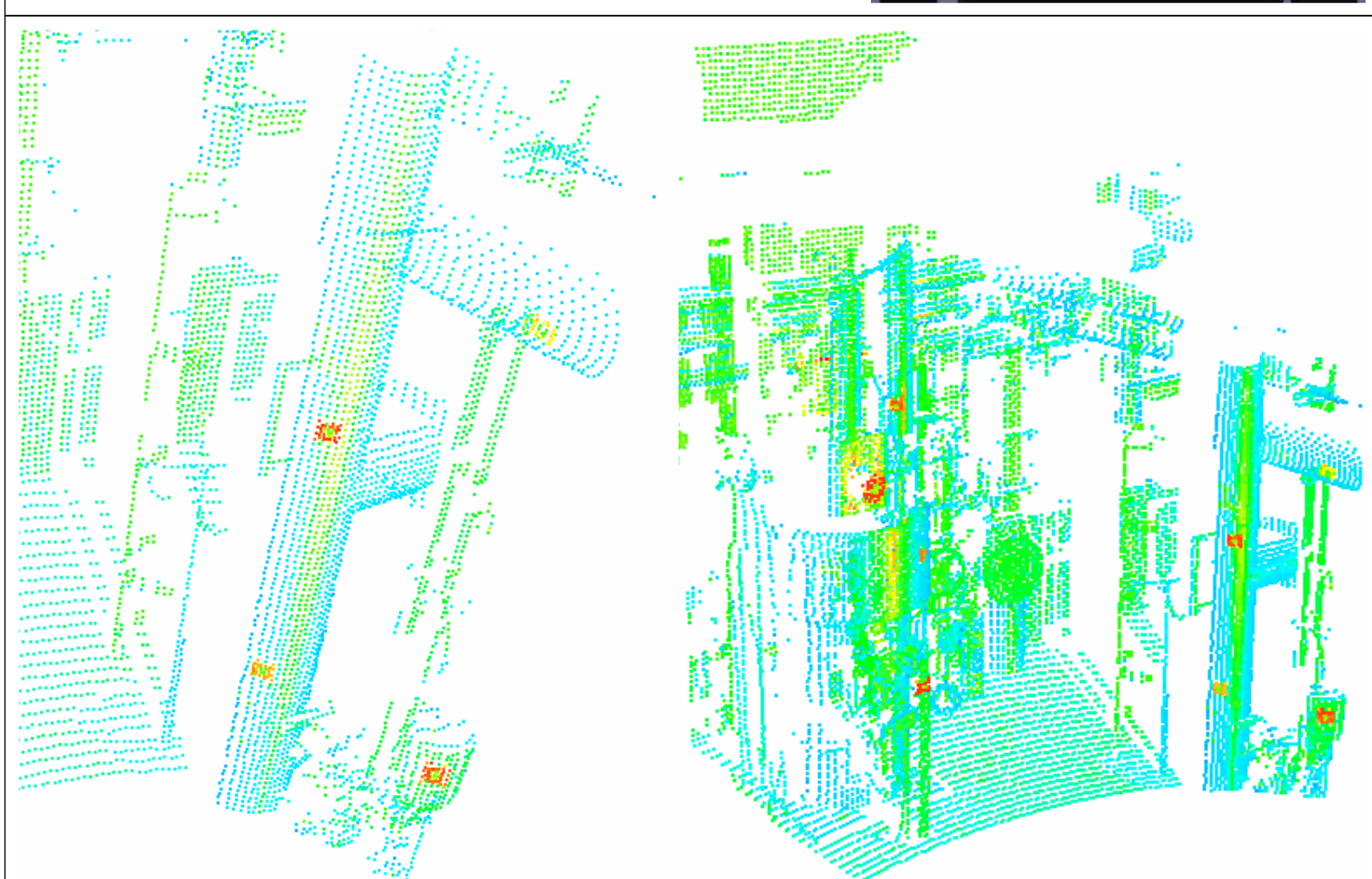
Leica HDS2500

- Principle: pulse round trip, laser wavelength: 532nm
- Range: up to 100m
Range accuracy: $\pm 4\text{mm}$
- Beam deflection: 2 mirrors
- Field of view: max $40^\circ \times 40^\circ$: “window” system
Angular accuracy: 0.00006rad
(3mm@50m)
- Spot size $\leq 6\text{mm}$ up to 50m
- Max scanning density:
0.25mm point-to-point spacing @50m
- Speed: 1000 pts/sec
- Max points: 1000col/2000row



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© Leica



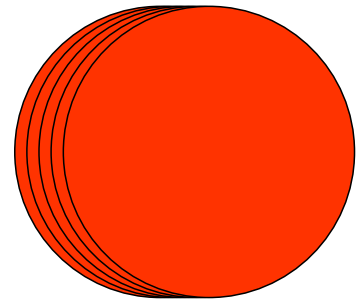
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Example data set



Example 1

Leica HDS2500



For distance 50m

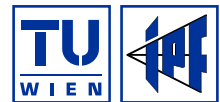
- Point accuracy $(\sigma_x^2 + \sigma_y^2 + \sigma_z^2)^{0.5} = \pm$ mm
- Spot size 6mm and point-to-point spacing 0.25mm
- 1000 points over 40°: point-to-point spacing 36mm



Speed

- 2000000 points in ½ hour
- Other factors
 - 10 scans for 1 panorama
 - Moving equipment: 20kg + 7kg power supply + laptop

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Example 2

Minolta Vivid 900

- Principle: triangulation with light
- Laser wavelength: 690nm
- Digital camera
 - CCD 640x480 pixels RGB
 - Pixel size: ~3.5µm
 - Focal length: 25mm, 14mm, 8mm
- Range: max 2.5m
- Scan time: 2.5 seconds
- Captures **color!**



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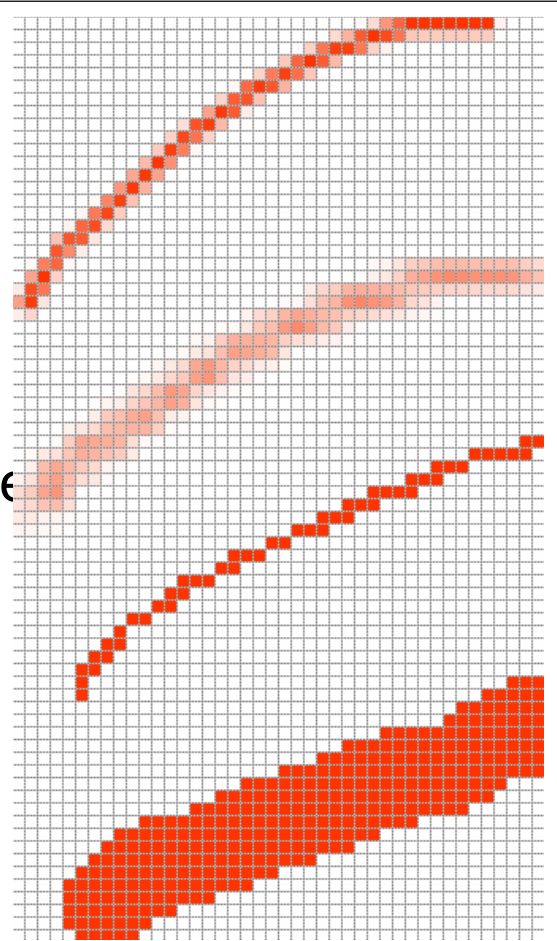
© Minolta



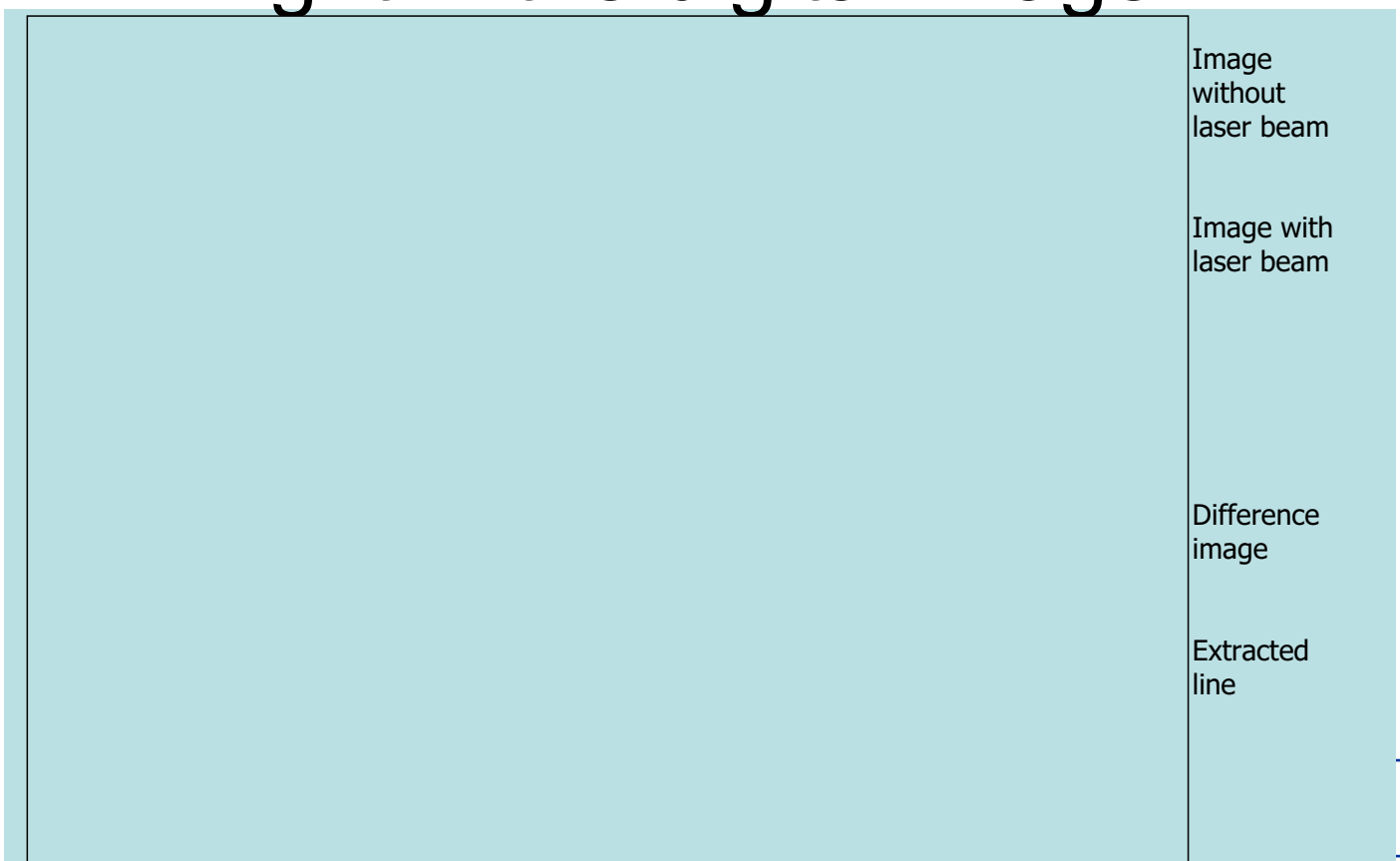
Example 2

Minolta Vivid 900

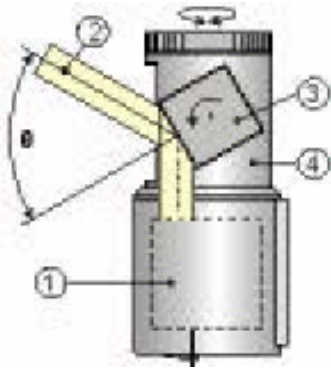
- For good color good lightning necessary
- How to find map of laser plane in digital image?
... see images on next slide
- Map of laser plane should be as thin as possible.
- How to achieve this?



Finding the map of the laser light in the digital image



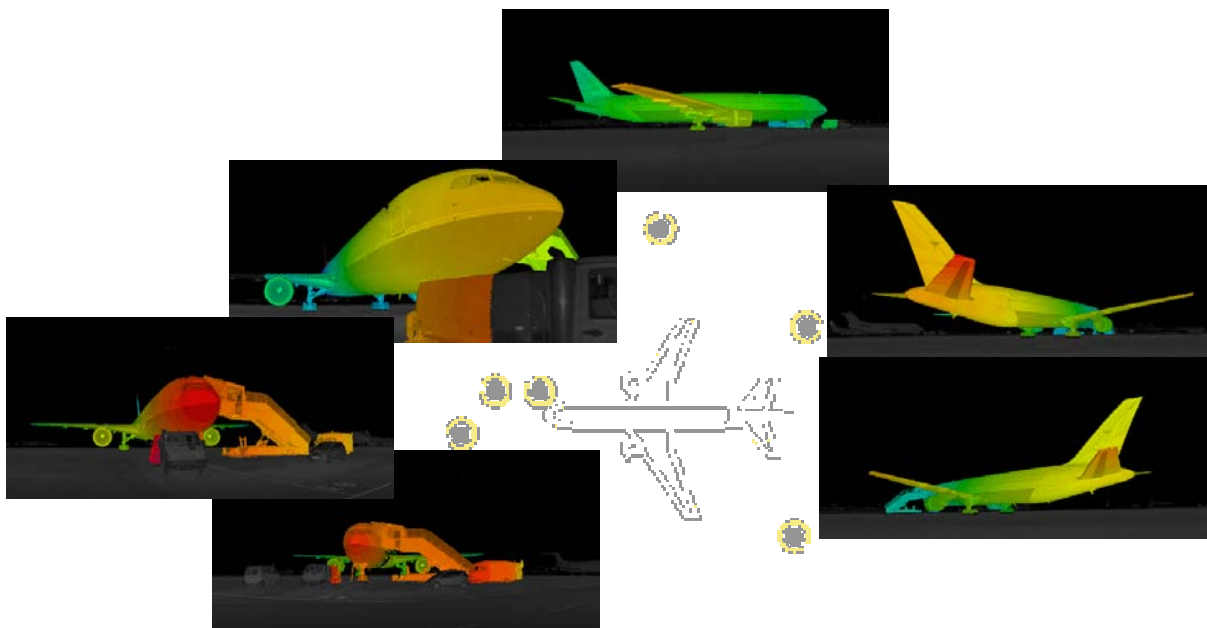
Example 3,4,5



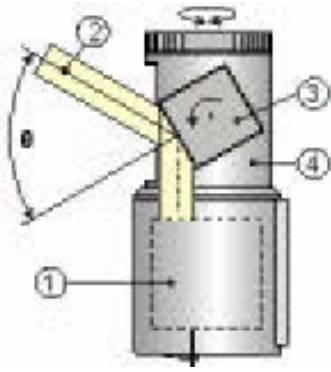
Riegl LMS Z420i

Pulse round trip,
rotating mirror +
instrument rotation

LMS Z210

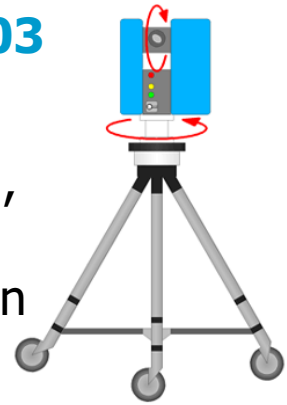


Example 3,4,5



Z+F Imager 5003
LARA 53500

Phase comparison,
rotating mirror +
instrument rotation



Riegl LMS Z420i

Pulse round trip,
rotating mirror +
instrument rotation

360°

Imager 5003

Intensity image

zenith

math. horizon

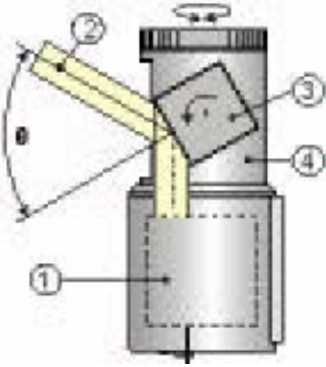
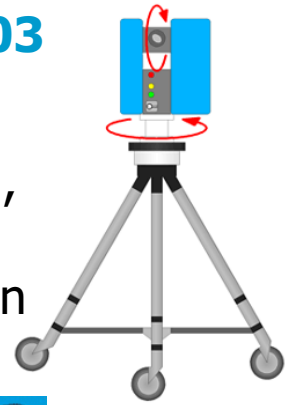
instrument base

Range image

Example 3,4,5

**Z+F Imager 5003
LARA 53500**

Phase comparison,
rotating mirror +
instrument rotation



Riegl LMS Z420i

Pulse round trip,
rotating mirror +
instrument rotation

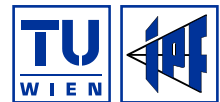


Mensi S10

Triangulation with laser
beam in plane,
+ instrument rotation

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© Riegl, Zoller+Fröhlich, Trimble



Competing Complementing Measurement Tools



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Comparison

terrestrial

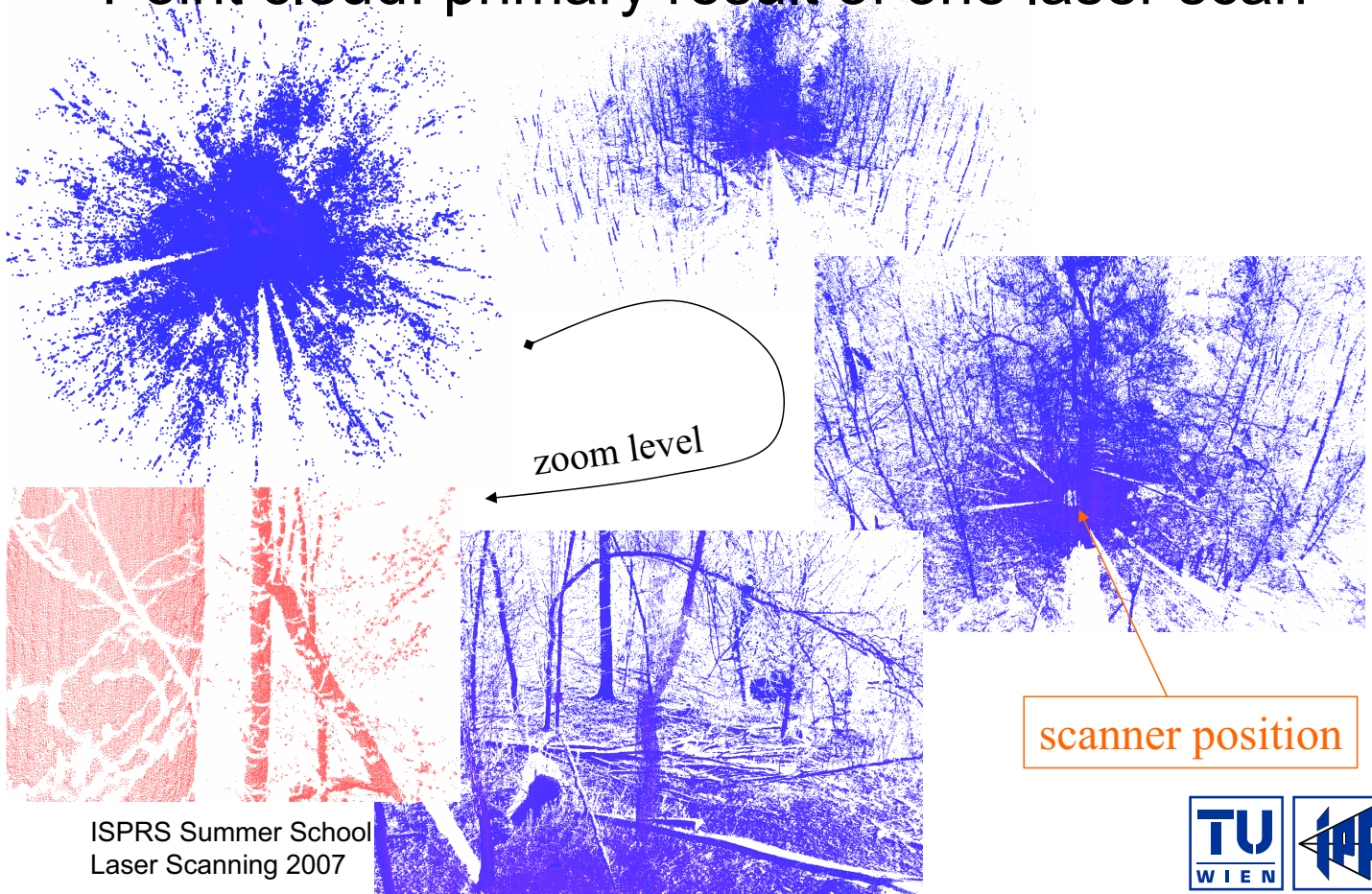
suited for measuring

	Satellite Positioning	CMM	Total Stations	Laser Scanning	Photo-grammetry
Points			x		
Edges			—		
Surfaces			—		
Range	global				
Precision					scale dependent
Speed					
Costs		very high			
Problems with/at Requirements					

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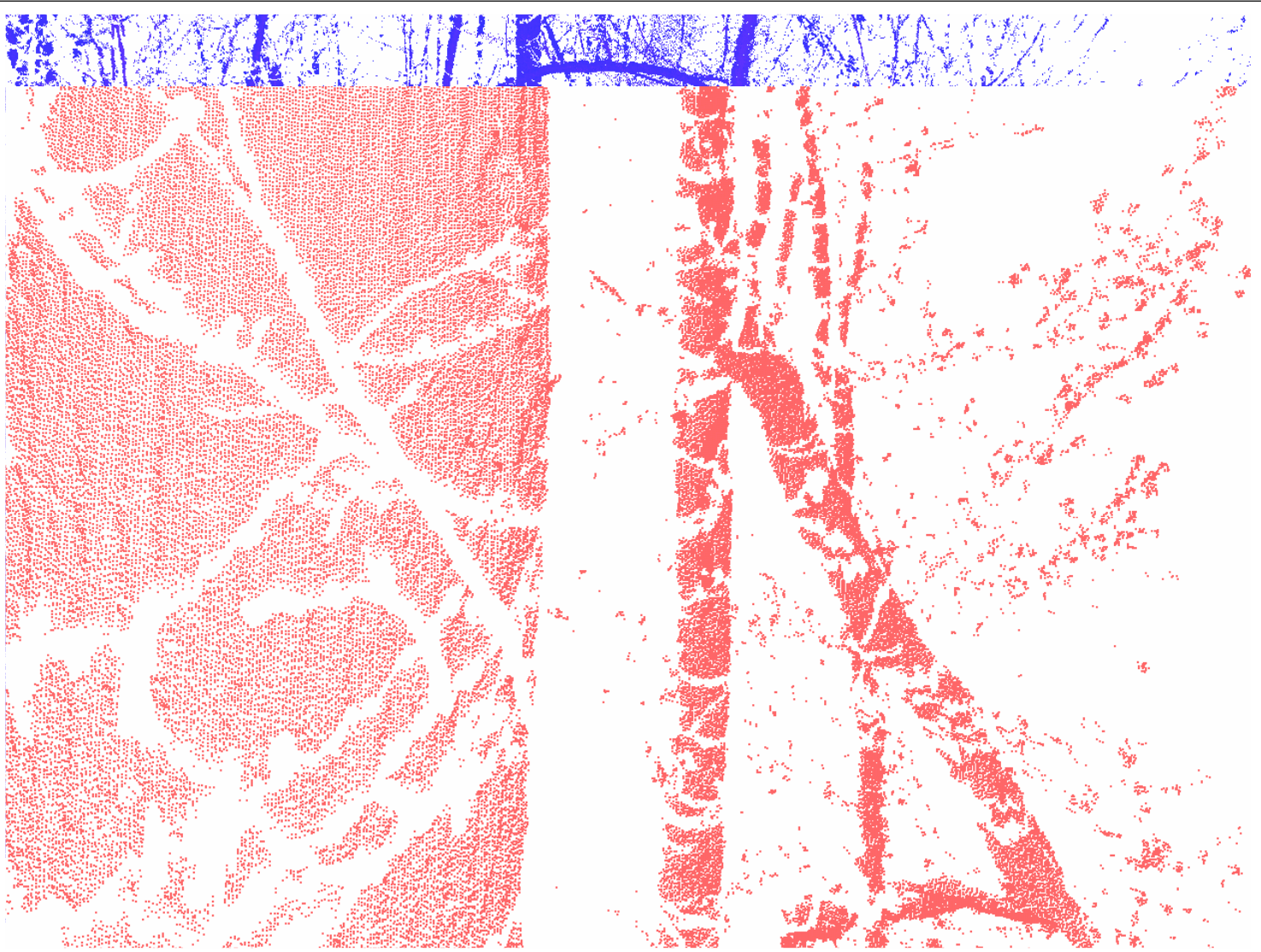


Point cloud: primary result of one laser scan



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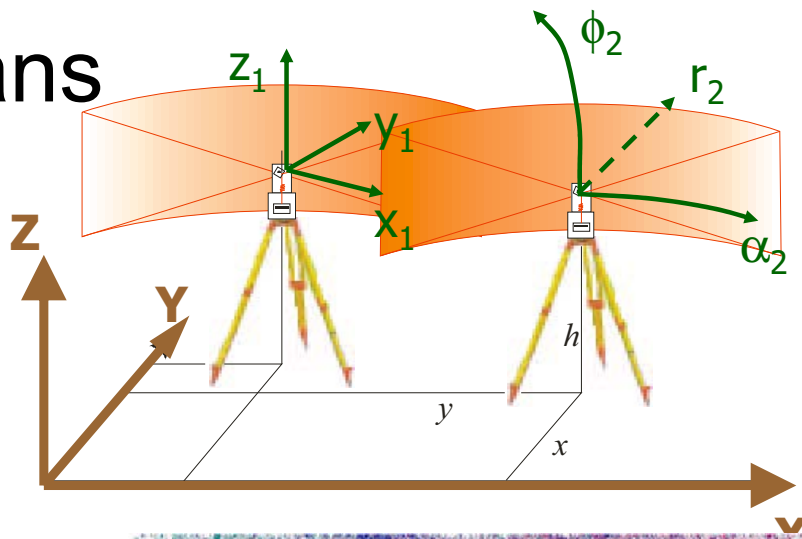




Registration

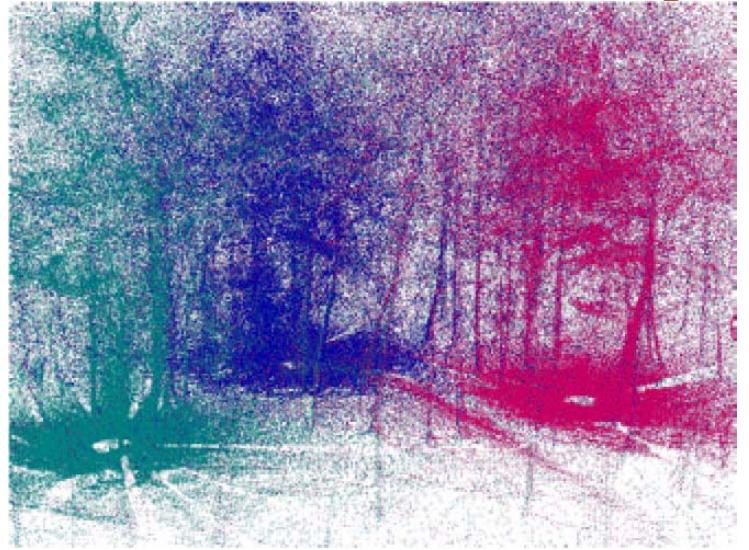
- 1. Object is visible only from one side in one scan
- 2. Multiple objects to be measured
- Different scans required to capture the entire scene
- Relative orientation (registration) required to have all points in one coordinate system
- Methods for Registration
 - Targets (like photogrammetry)
 - Iterative closest point (ICP)
 - Object based (corresponding features, e.g. planes, cylinders, ...)
 - Direct georeferencing
- Fine vs. coarse orientation

Combining scans



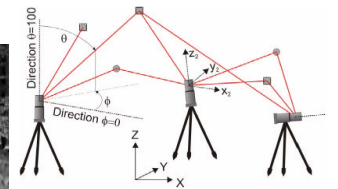
- = relative orientation
- = registration
- = consolidation
- = alignment
- = co-registration

Transform **each local device**
co-ordinate system into
one superior system.



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Registration methods



- Tie points

- ➔ -) extra effort, only close to ground (extrapolation)
- ➔ +) applicable in almost all circumstances

- ICP (iterative closest point)

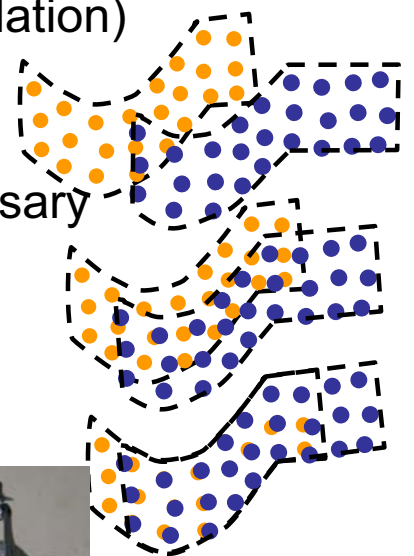
- ➔ -) overlap and manual approximation necessary
- ➔ +) uses entire point cloud

- Object based: parametric "Features"

- ➔ -) found only in special cases (corners, cylinders)

- Direct georeferencing

- ➔ -) low cost devices: insufficient precision
- ➔ +) highest degree of automation

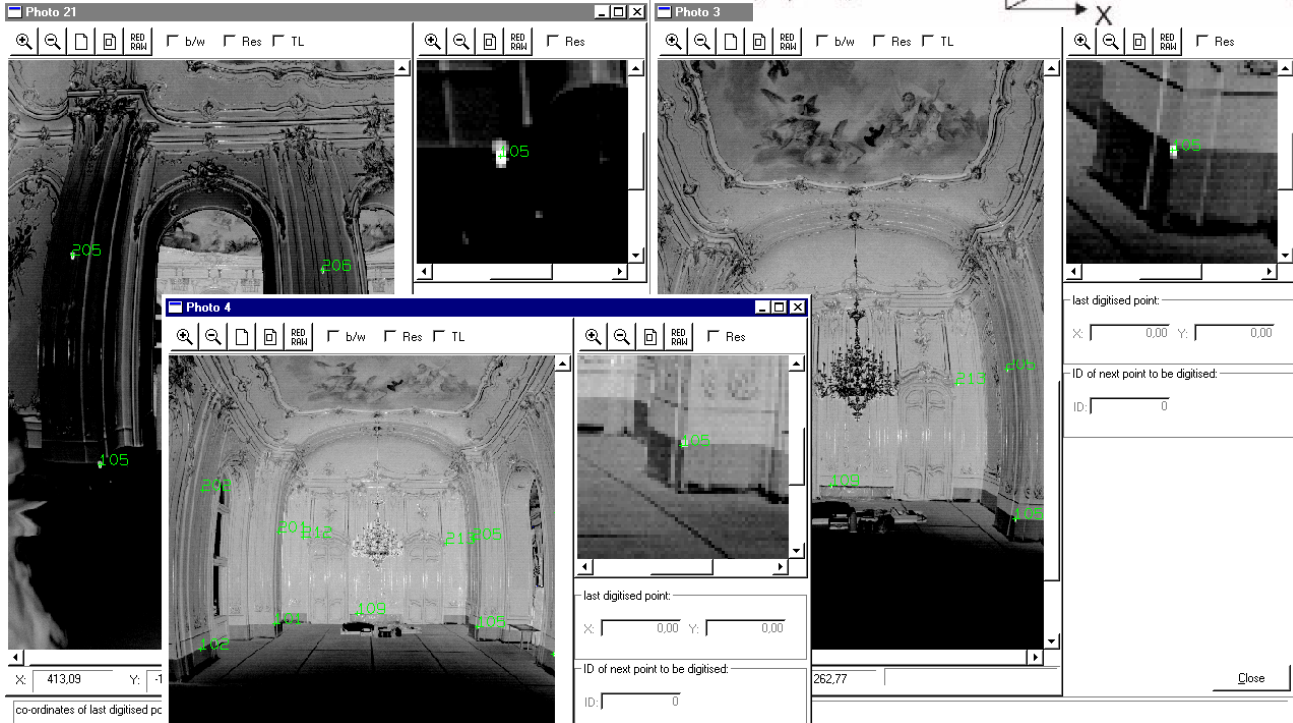
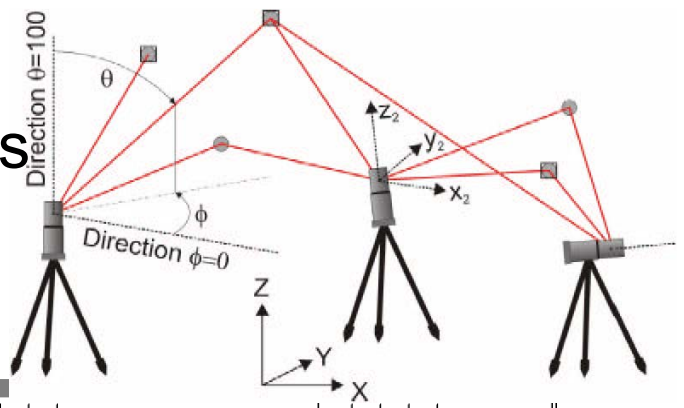


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Böhm, Haala: EFFICIENT INTEGRATION OF AERIAL AND TERRESTRIAL LASER DATA FOR VIRTUAL CITY MODELING USING LASERMAPS. ISPRS WG III/3, III/4, V/3 Workshop "Laser scanning 2005", Enschede, the Netherlands, September 12-14, 2005

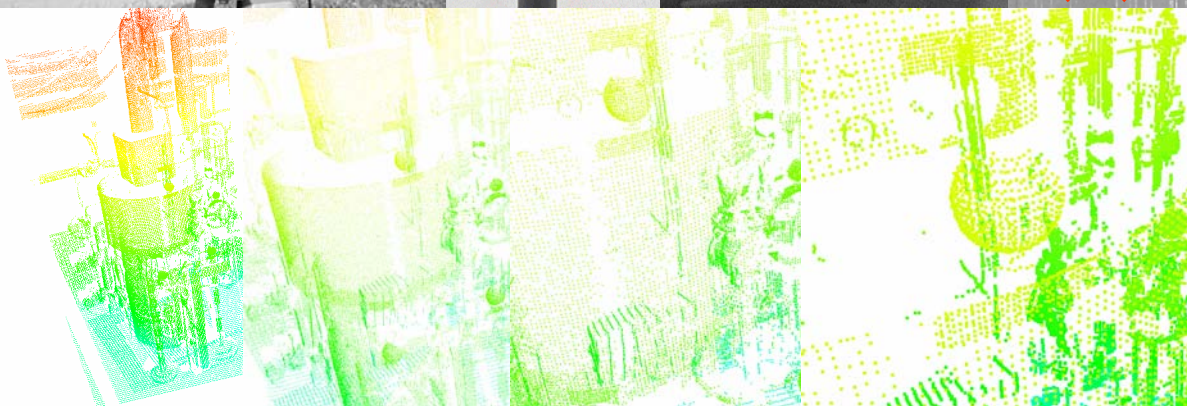
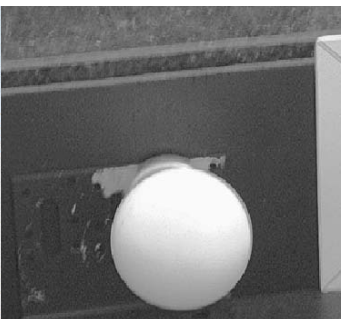
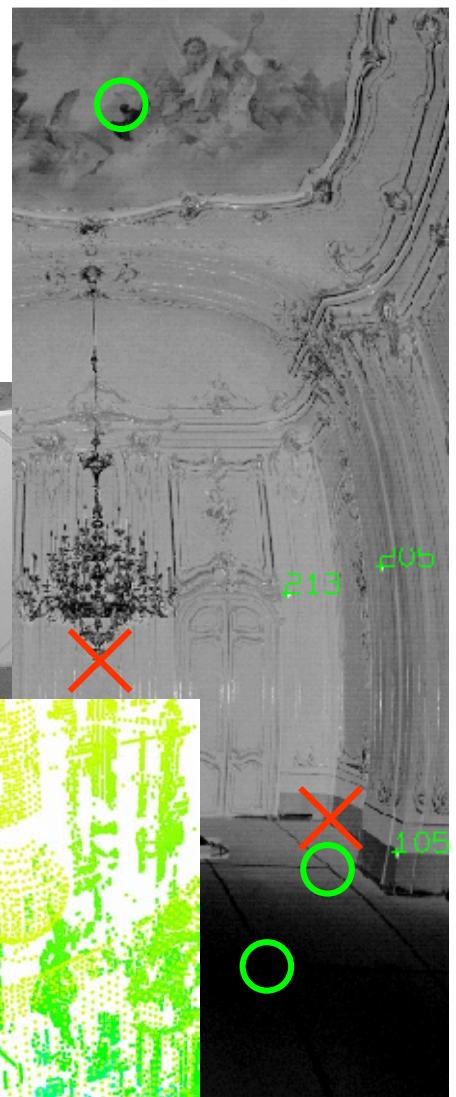
Registration via tie points

Example: 3 scans
retro-reflective targets (2cm)



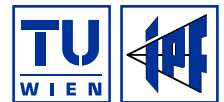
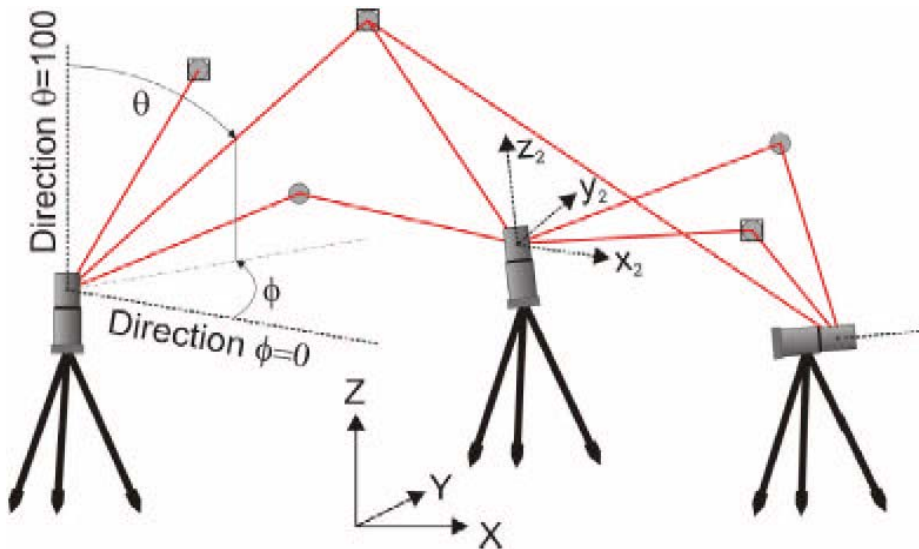
Registration via tie points

- Signalized vs. natural points
- Identify in Intensity image OR Range image OR Point cloud



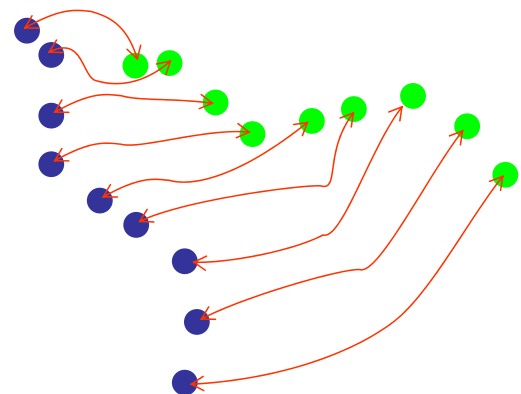
Registration via tie points

- Identify with sub-pixel accuracy
- Can be observed in photos or by tacheometry
- How many tie points required to register 2 scans?



Registration with ICP

- Given: 2 point clouds
 - on the same surface
 - in different local coord.sys.
- Simple case
 - correspondences between points
 - exist
 - are known
- Solution



$$\sum_{i=1}^n \|q_i - (t + \mathbf{R}p_i)\|^2 \rightarrow \text{Minimum}$$

How to?

Registration with ICP

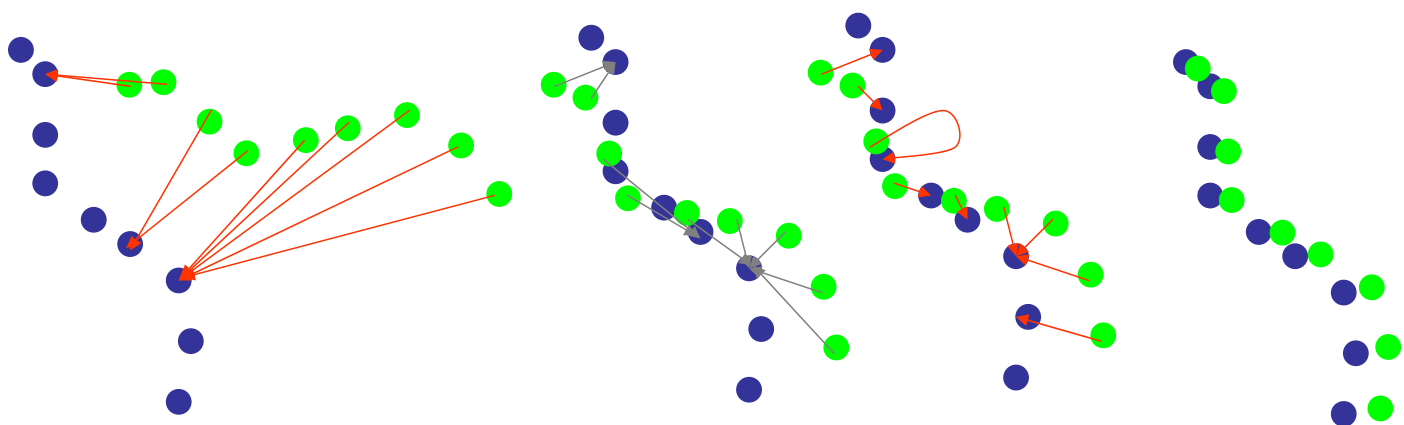
Problems

- Correspondences are generally not known
- Point-to-point correspondences do NOT exist

Solution

- Replace: Corresponding point \rightarrow closest point
- Solve for transformation parameters
- Iterate

Registration with ICP



Find for each p_i closest point in $Q = \{q_1, \dots, q_m\}$

Solve for and apply t and R to minimize offsets

Find for each p_i closest point in $Q = \{q_1, \dots, q_m\}$

...

Registration with ICP

- num. pts. in Q \neq num. pts. in P
- Rough alignment required (manual)
- Needs many iterations
- Works bad for flat surfaces
- Requires many iterations

- But! No tie points required!

Additional Notes

All points or only short distances (10% of all distances)

Alternative approaches:

1. Subsample one point set
2. Distance to triangulation
3. Distance to estimated tangent planes

Registration via objects

- (Points)
- Planes
- Lines

- Advantages / disadvantages

Coarse registration

- Esp.: generate approx. values for ICP
- Comparable to automatic relative orientation of an image pair
- Extraction of features
- Correspondence hypothesis
- Evaluation

Current ressearch topic !

Model reconstruction

- Point cloud
 - Many points
 - Without semantic information („meaning“)
 - Quality
- Model
 - Captures relevant aspects of reality
- Types of models
 - Meshes/Tiangulation
 - Boundary representation
 - Primitive instancing



Object size	Accuracy
1-5m	±0.2mm
5-50m	±1mm
50-1000m	±1-10cm
Airborne	
100-300m	±5cm
up to 2000m	±20cm

Modeling

Measurement → Registration → Set of point clouds in one co-ordinate system

Modeling strategies

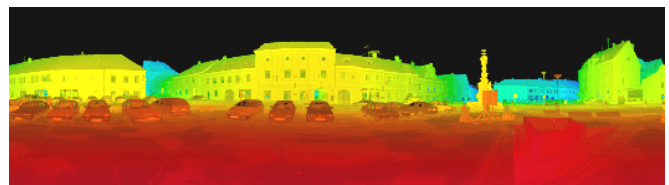
1. Point cloud is final product
or extract information directly from point cloud
2. Generate mesh (triangulation)
 - Triangulate visible parts
 - Generate water tight model
3. Make parametric models (primitive instancing)
4. B-Rep model generation
5. Generate free form surfaces (NURBS, ...)

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Point Cloud as Final Product

- Visualization
 - Give points a size
e.g. 2 pixel or 2cm
 - Texture from photo
- Interface checking
- Simple measurements

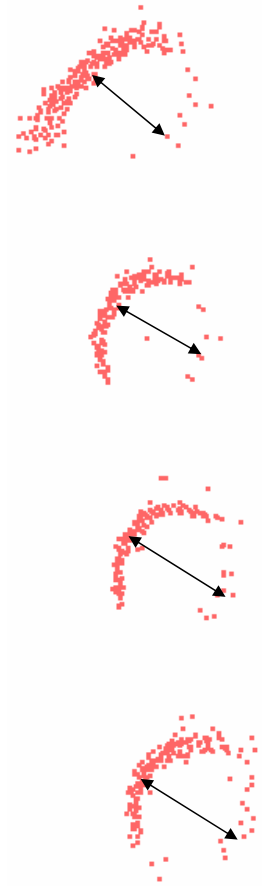
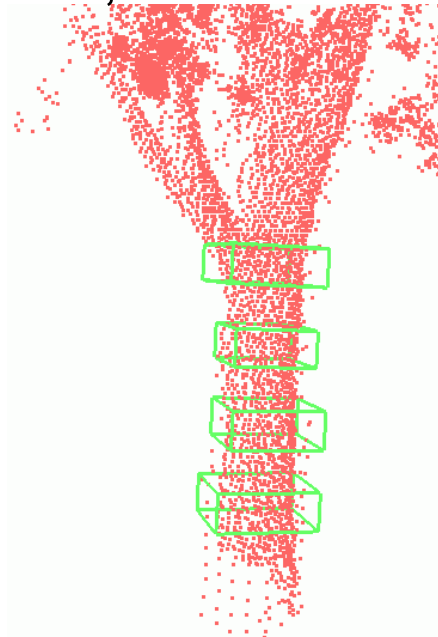


Yellow: point cloud,
gray: planned installation © Rieg, Leica



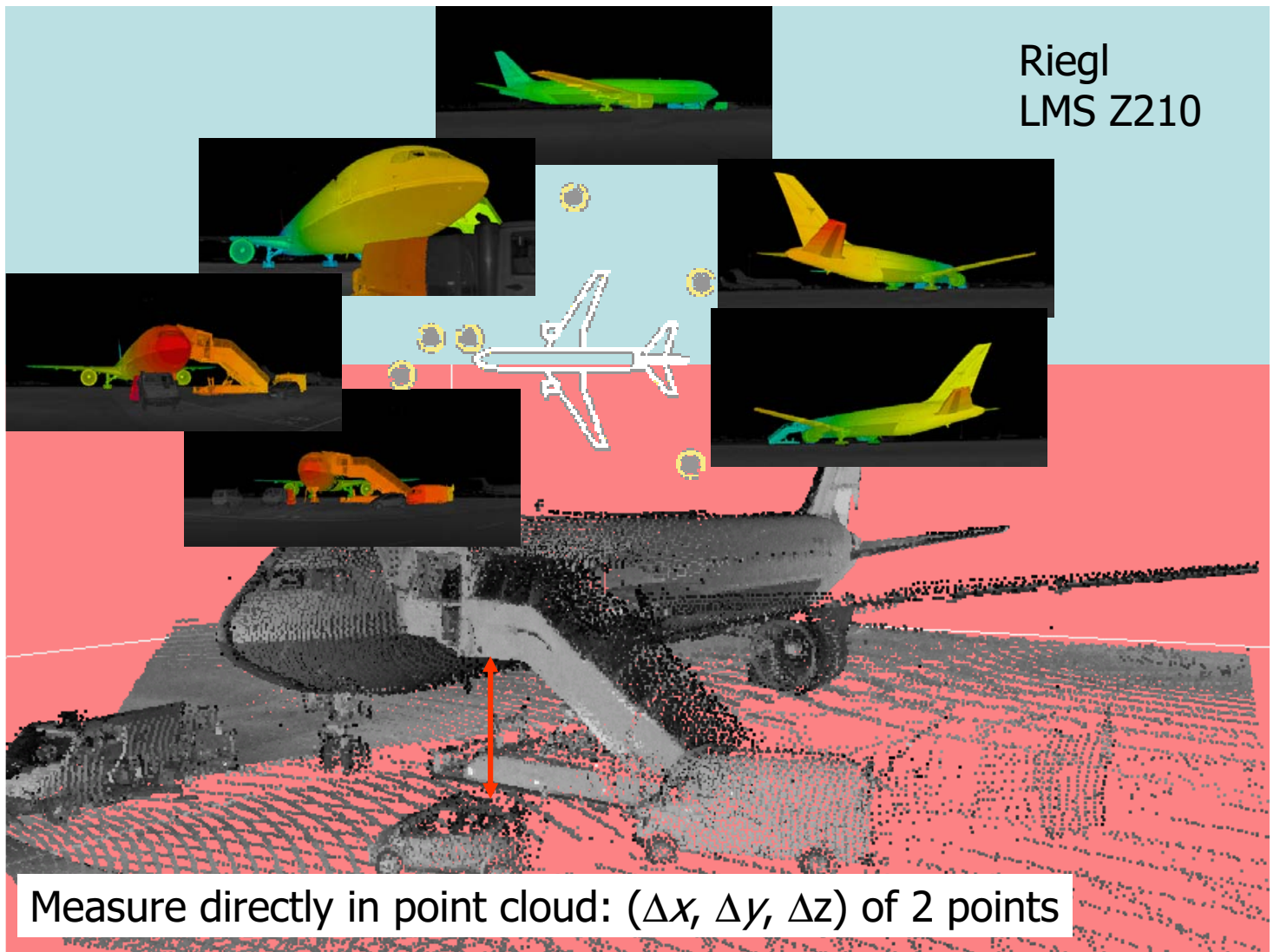
Products extracted from point clouds

Example: tree cross sections, diameter measurement



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Riegl
LMS Z210



Measure directly in point cloud: $(\Delta x, \Delta y, \Delta z)$ of 2 points

Triangulation / Meshing

Triangulation **adds surface** to point cloud

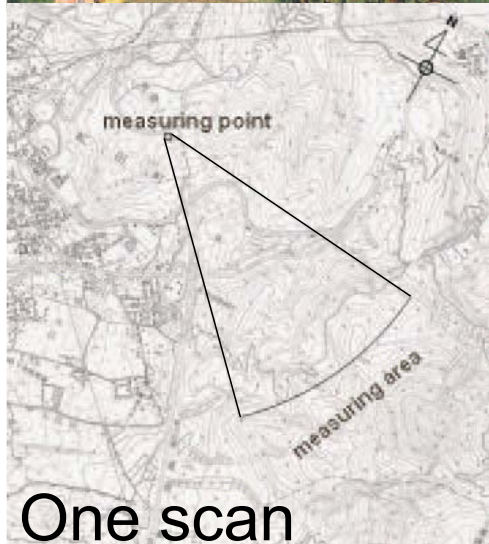
- Surface area computation
- Interpolation between points
- Computation of surface properties
tangent plane, curvature, ...
- Intersection with other surfaces
e.g. with planes for cross sections
- Triangulate in
 - ground plan
 - parameterization domain
 - 3D
- Basis for freeform surface modelling
- Better combination with texture from images

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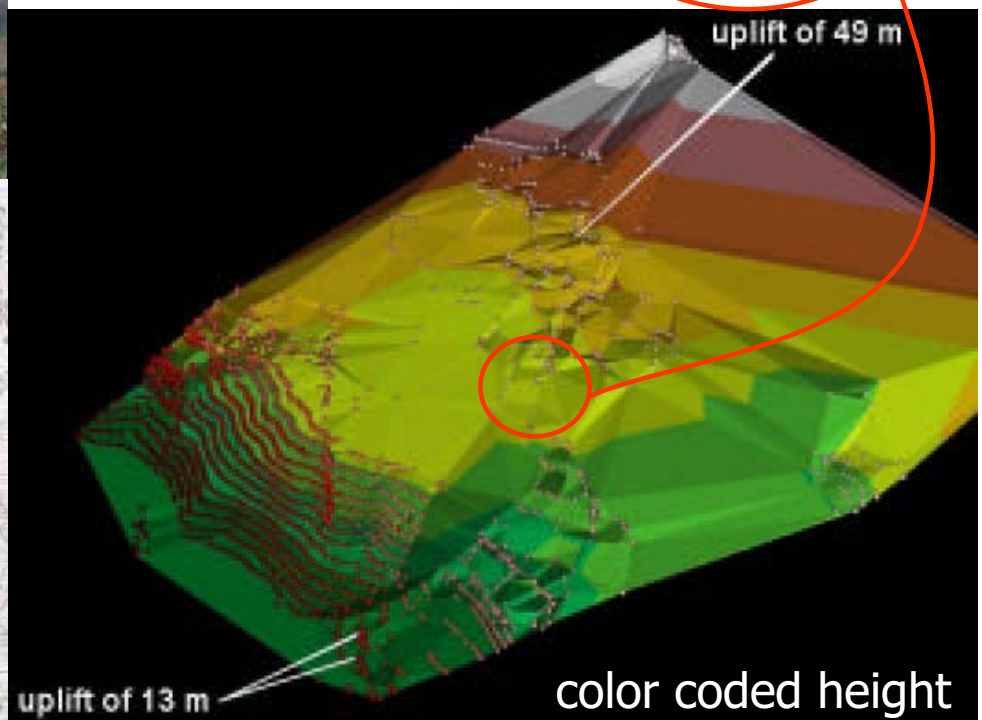
Triangulation in ground plane

Monitor volcano

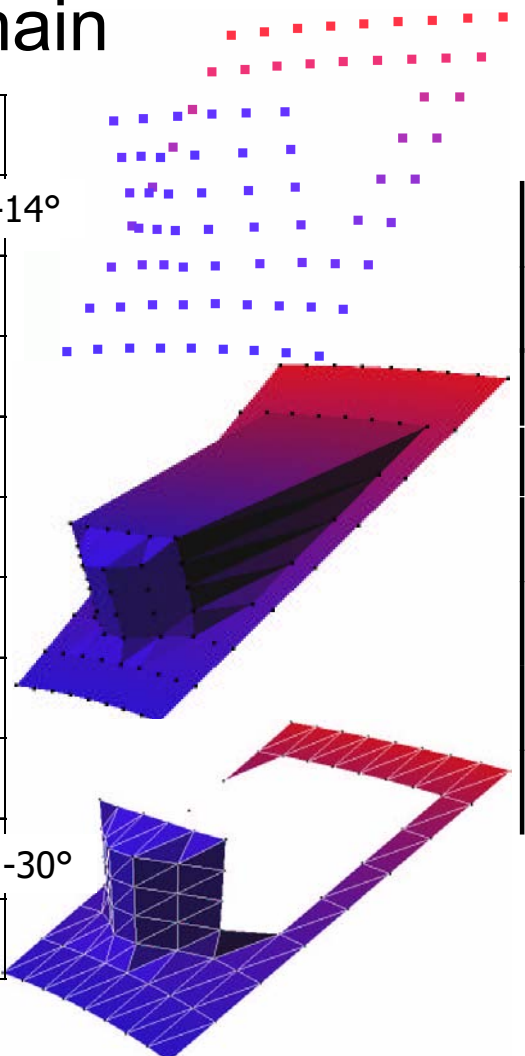
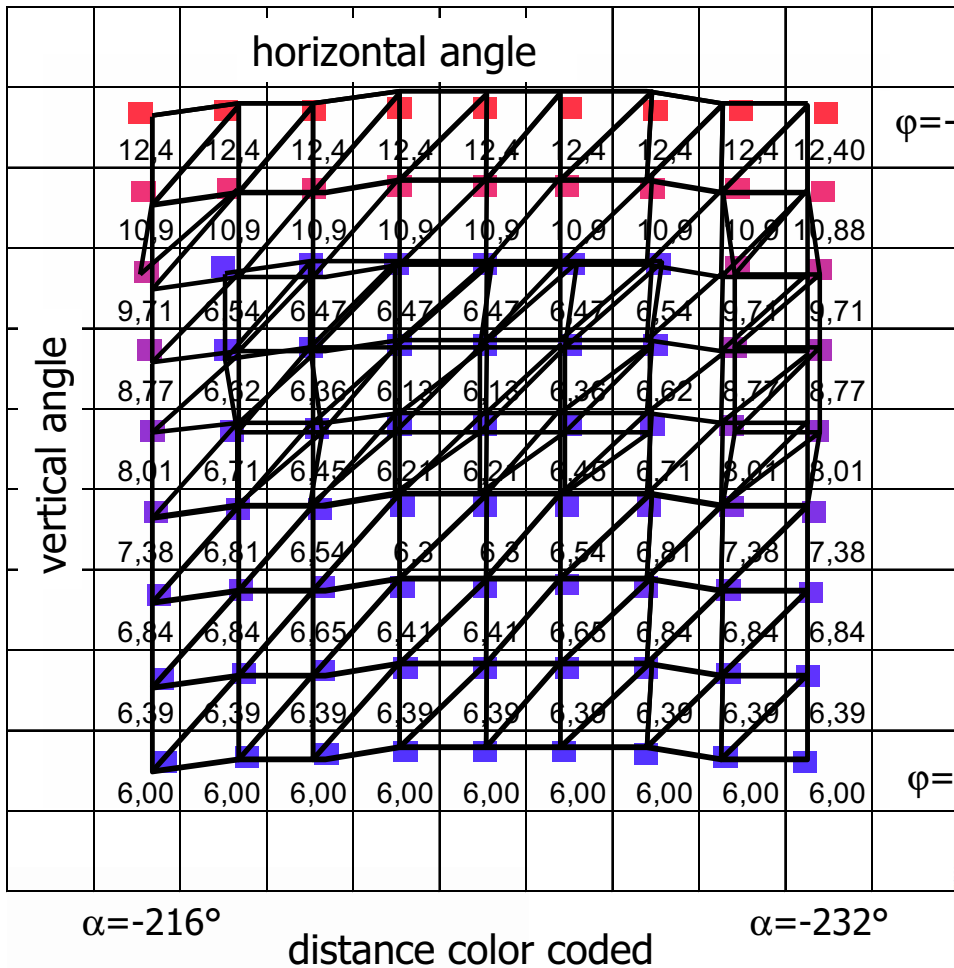


One scan

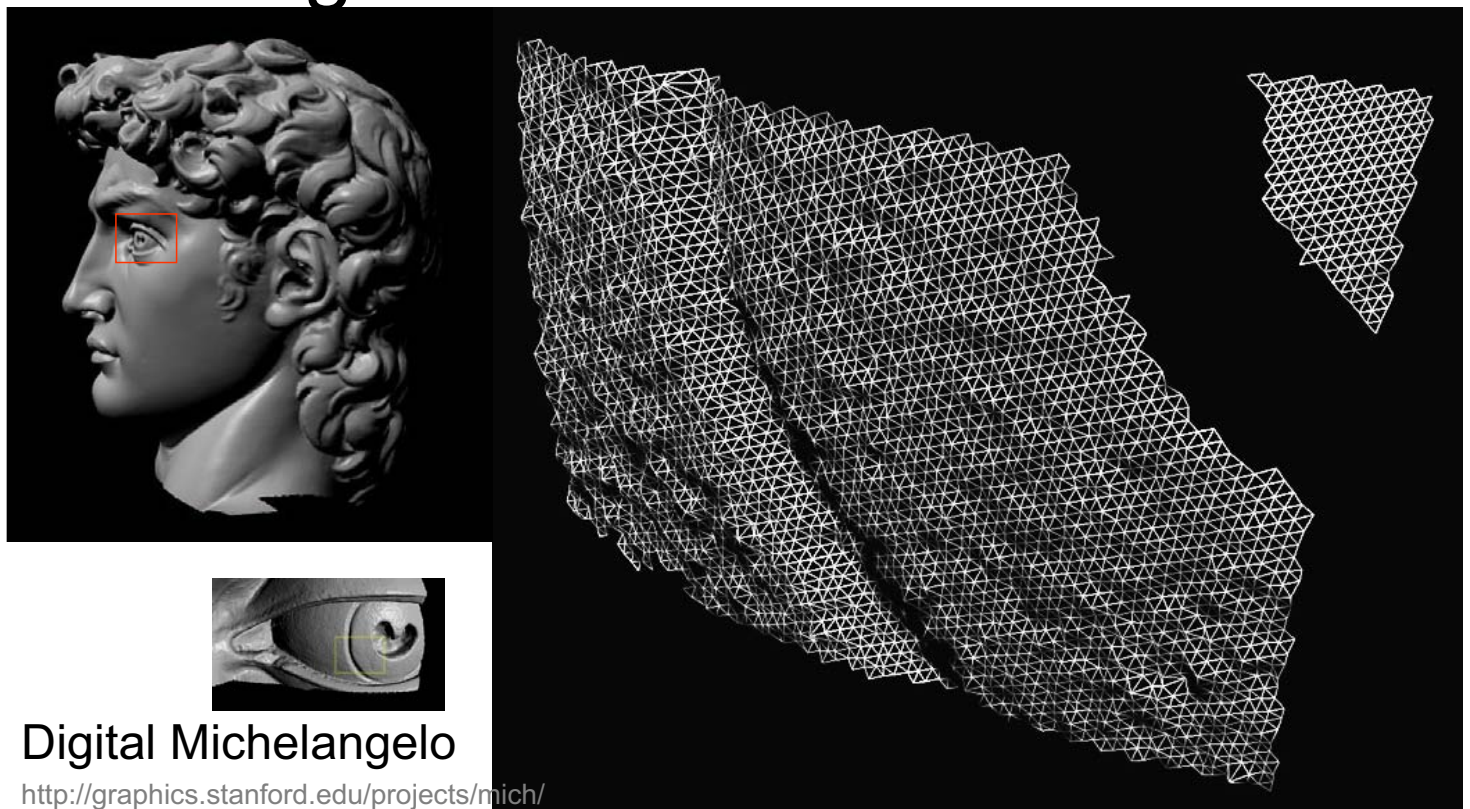
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Triangulation in scanner domain



Triangulation in scanner domain



Digital Michelangelo

<http://graphics.stanford.edu/projects/mich/>

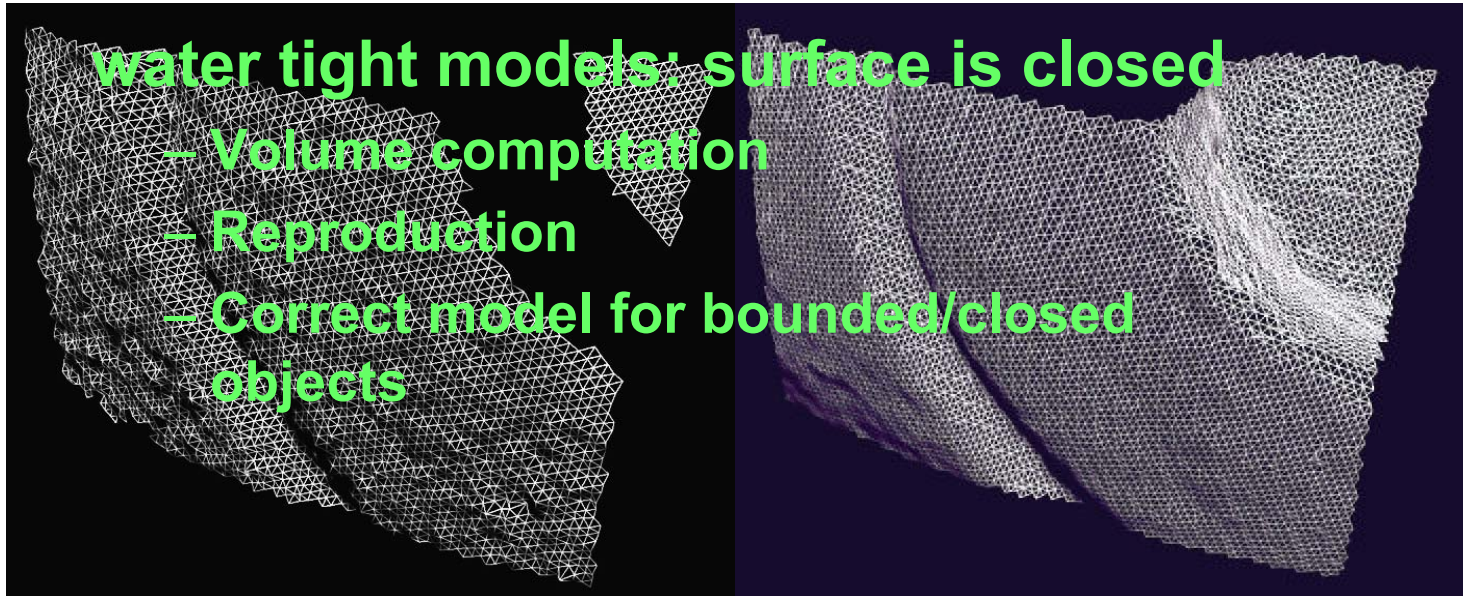
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Triangulation

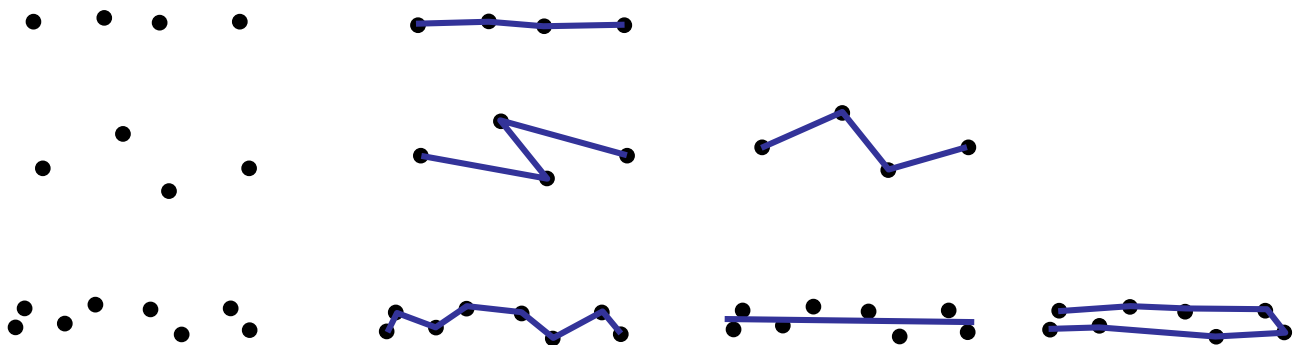
Complex objects require more scans: different sides & occlusions

1. Combine triangulations of individual scans
→ real 3D triangulation
2. Fill holes
no holes → water tight model



Triangulation in 3D

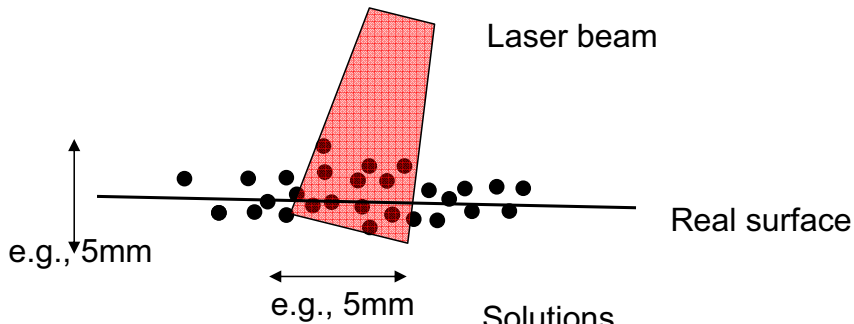
- Problem: which points are neighbors ?



Schematic 2D view

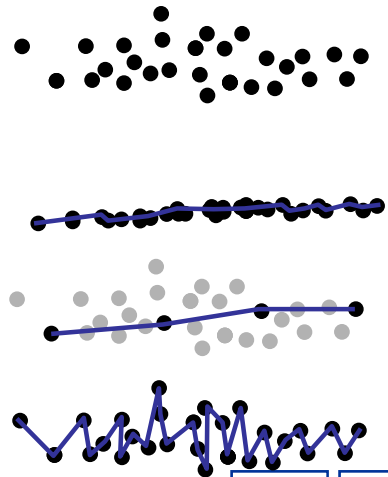
Triangulation and Noise

Random measurement errors and measurement density

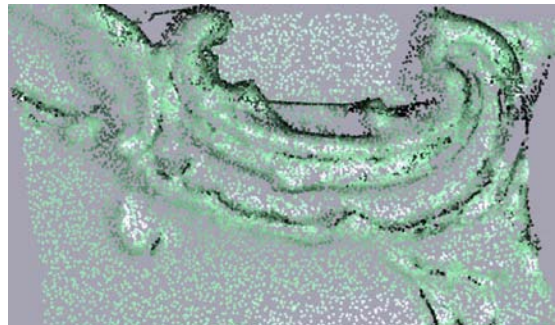
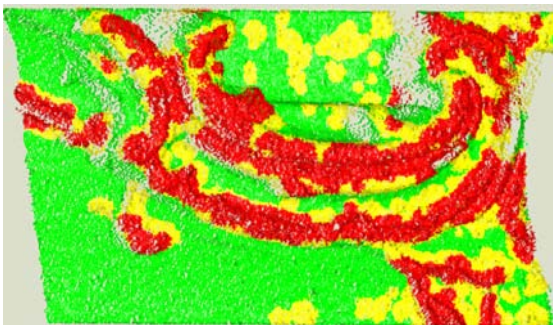
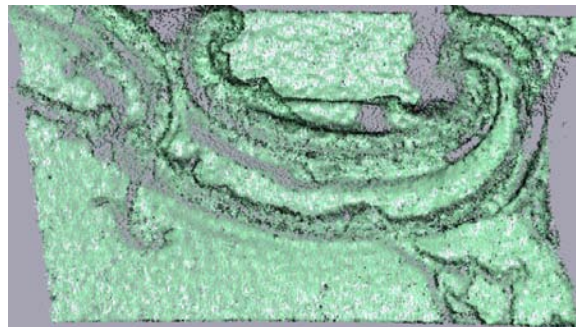


- Remove noise: low pass filter
- Thin out point cloud
- Robust methods

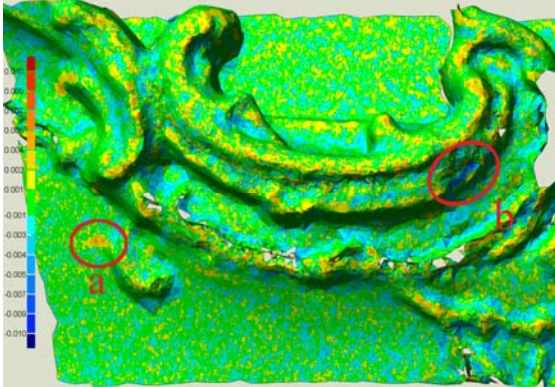
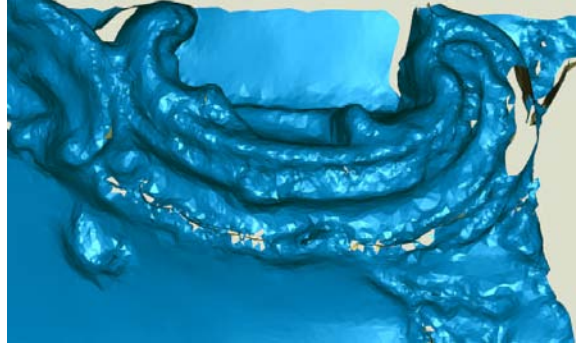
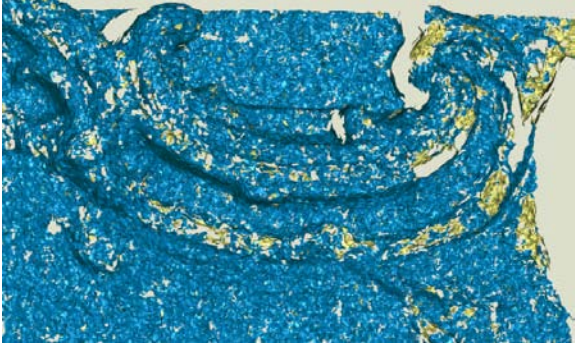
Triangulation ?



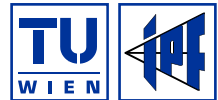
Triangulation and Noise



Triangulation and Noise



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Triangulation Example

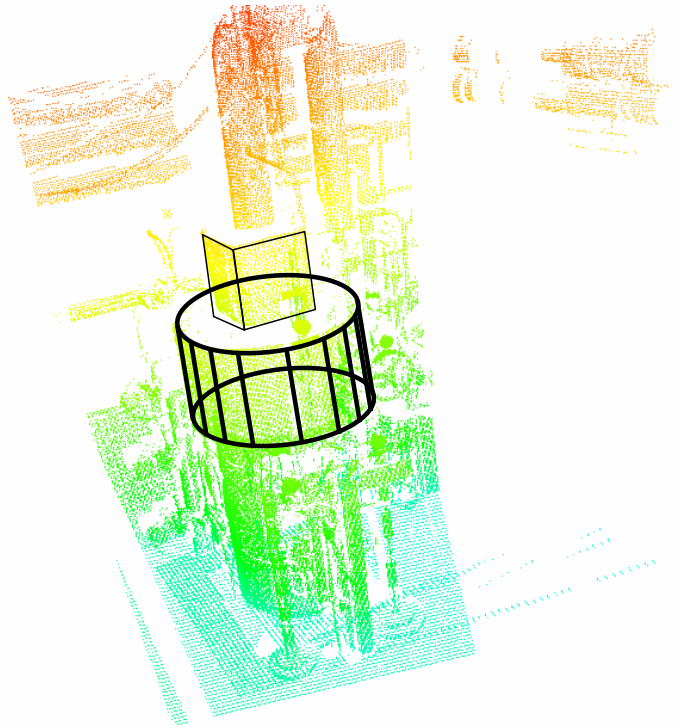


Parametric Primitives

Man-made structures

planes, cylinders, spheres, tori, cones, ...

- Select points manually/automated
 - Select primitive type
 - Least squares fit determines primitive parameters
- How to? derivation of plane ...



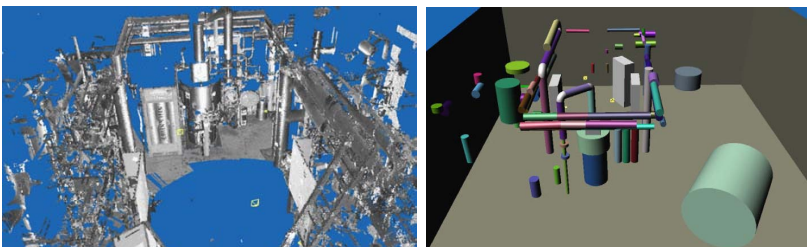
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Parametric Primitives

Automation through

- Segmentation of point cloud
e.g. region growing based on normal vector similarity
- Identification of surface type
e.g. Gaussian image (normal vector image)

Point cloud \rightarrow Model



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Boundary representation models

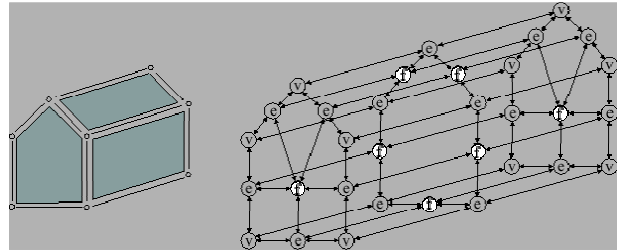
Generating B-Reps

- Digitizing in point cloud / mesh

point identification

edge = connect of 2 *points*

face = enclose by *edges*



- Similar to photogrammetry, but !!!: digitizing in one scan is sufficient

- Example: AutoCAD plugin digitizing a point and a line



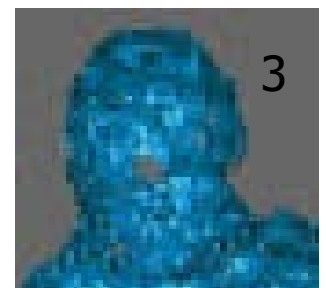
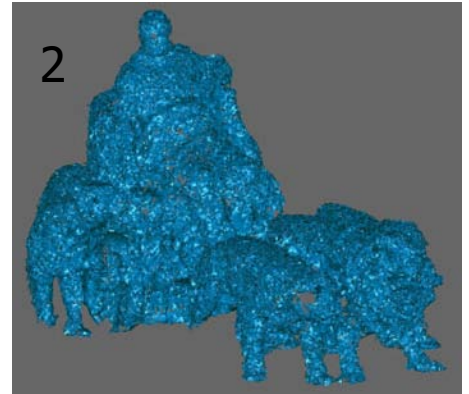
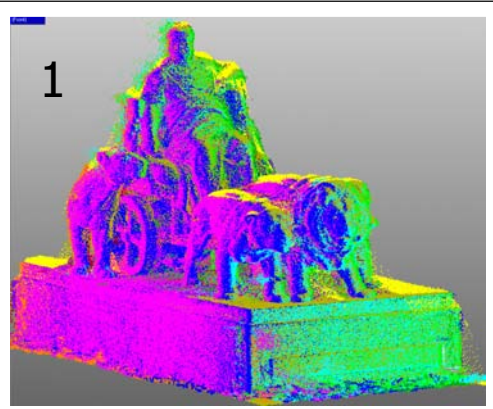
Free form surfaces

Modeling with free form surfaces

- What are free form surfaces?
= splines, but bivariate
- Surfaces controlled by a (low) number of parameters, with continuity constraints (e.g. C1, tangent plane continuity) between adjacent surface patches
- NURBS = Non-uniform rational B-splines

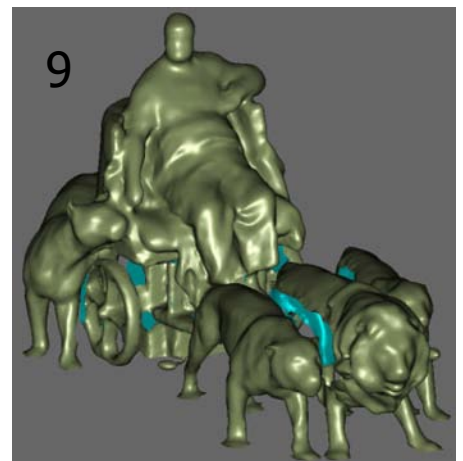
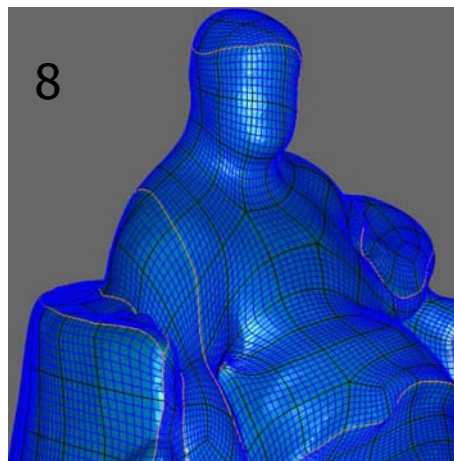
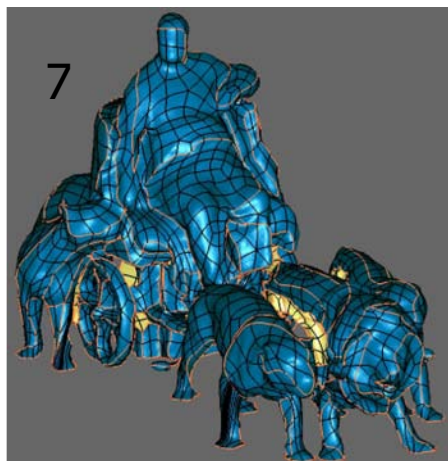
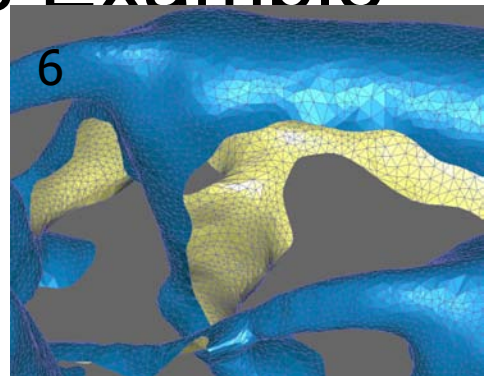
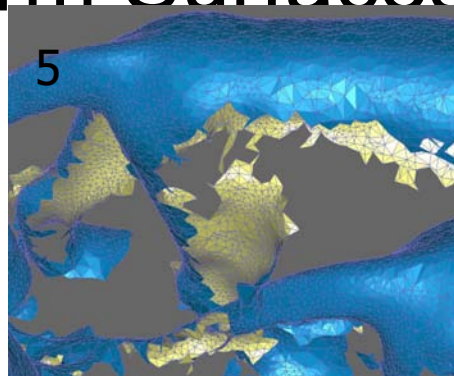
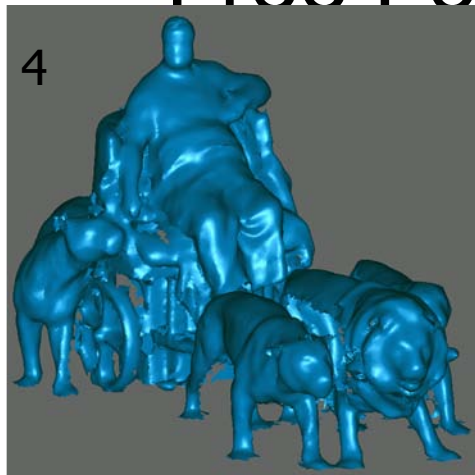
Free Form Surfaces Example

1. Original point cloud (~10 scans)
2. Triangulation (very rough surface)
3. Detail of triangulation (head)
4. Smoothed triangulation
5. Irregular boundaries of surfaces
6. Smoothed boundaries, hole-filling
7. Patch layout
8. Detail of patch layout
9. NURBS fitted to patches (i.e. point sets)



1
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Free Form Surfaces Example



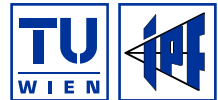
Applications

- 3D Visualization
- Archeology
- Architecture and Façade Measurement
- Archiving: Historical, Legal
- As-built Surveying
- City Modeling
- Digital Factory
- Forest Management
- Forensics
- Infrastructure
- Interface checking
- Medical Imaging/Medical Applications
- Mining/Open Pit Mining
- Movie Industry
- Monitoring and Civil Engineering
- Power Line + Poles Measurement
- Preservation
- Process Automation and Robotics
- Profiles, Volumes, Area calculations
- Quality Control/Quality Assurance
- Rapid Prototyping
- Reverse Engineering
- Rock Face Analysis
- Topography
- Tunnel Surveying
- Urban Planning
- Virtual Reality

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Taken from Rieg, Optech, Z+F, Leica



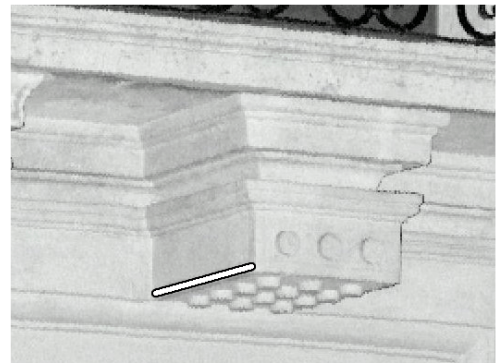
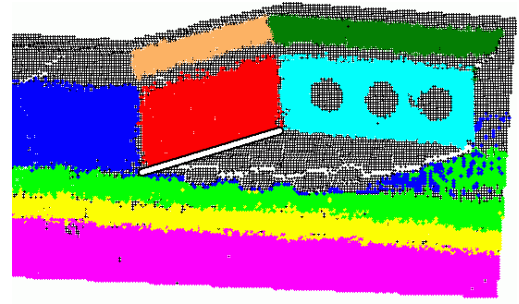
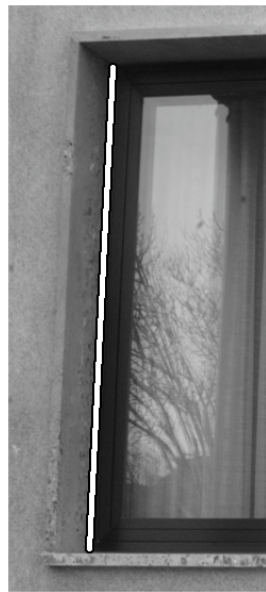
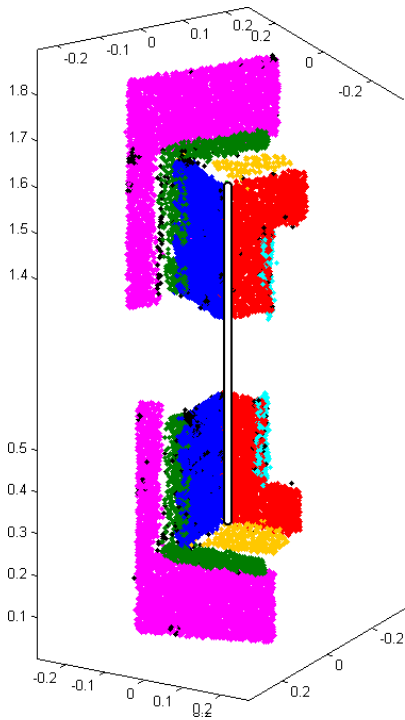
Applications

In the following slides example applications
will be presented

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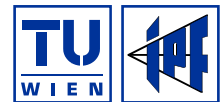
Measurement in Models



Window height: reference = 1447mm ; measured: 1444mm

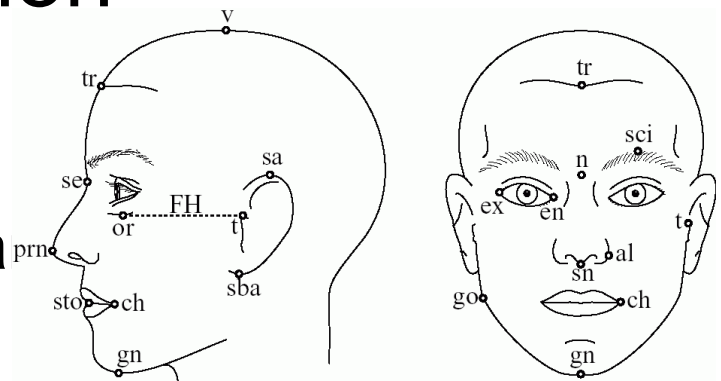
Base: ref. = meas. = 518mm

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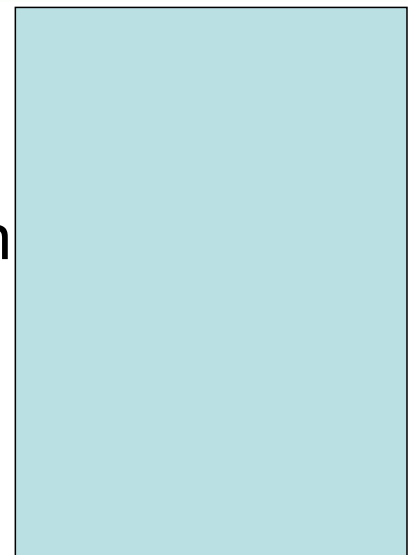
Medical Application

Measurement of anthropometric landmarks in the (human) face



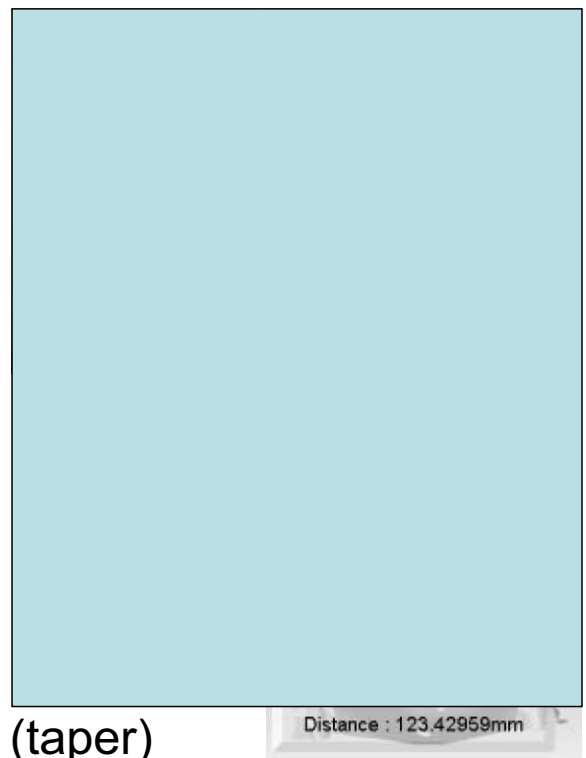
- Comparison pre/post operation
- Monitor change during evolution
- Guarantee identity of persons
- ...

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Medical Application

- Which type of scanner? Why?
- Processing of data:
use point cloud or simple mesh
- Degree of automation:
manual selection of landmarks
- Problems:
- Advantage over current method (taper)
Scan once → Points → measure any landmark
anytime
non contact method



Distance : 123.42959mm

Heritage Application

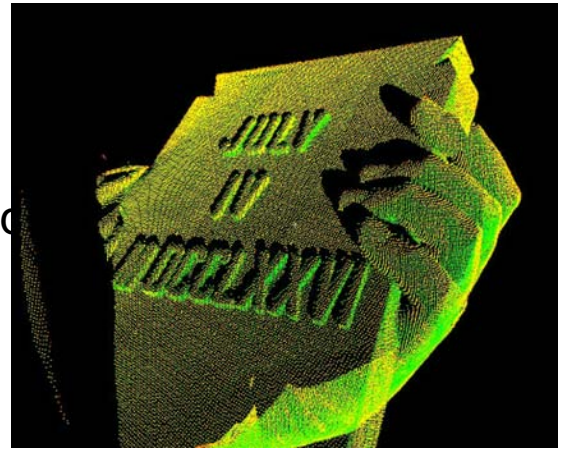
DSOL (http://www.arch.ttu.edu/digital_liberty/)

- Preservation
digital statue is “eternal”
- Simple measurements,
e.g. crown diameter
- Investigation of
corrugation, analysis
of structural, mechanical
problems
- Available everywhere,
make (small scale) models



Heritage Application

- Which type of scanner? Why?
- More than one positioning needed
- Problems:



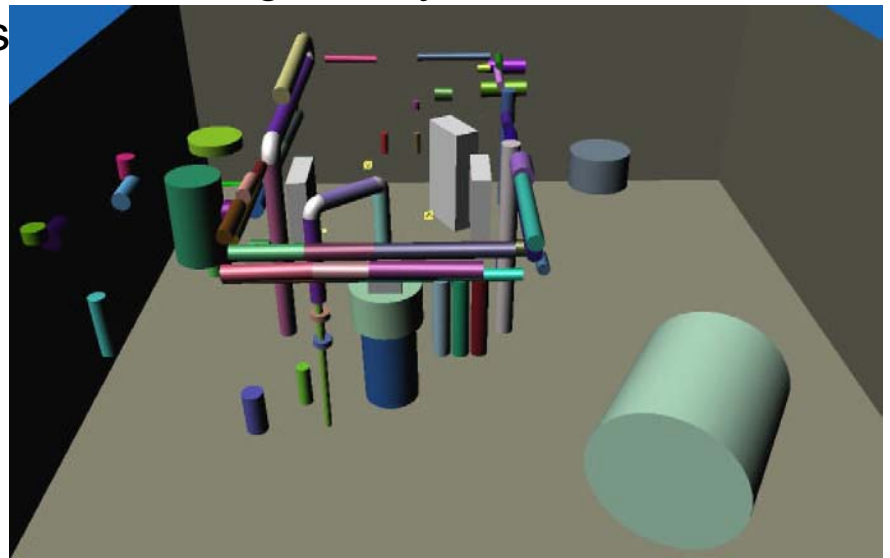
- Modeling
combine different scans
make TIN model
texture:
- Alternative methods:



Factory Reconstruction

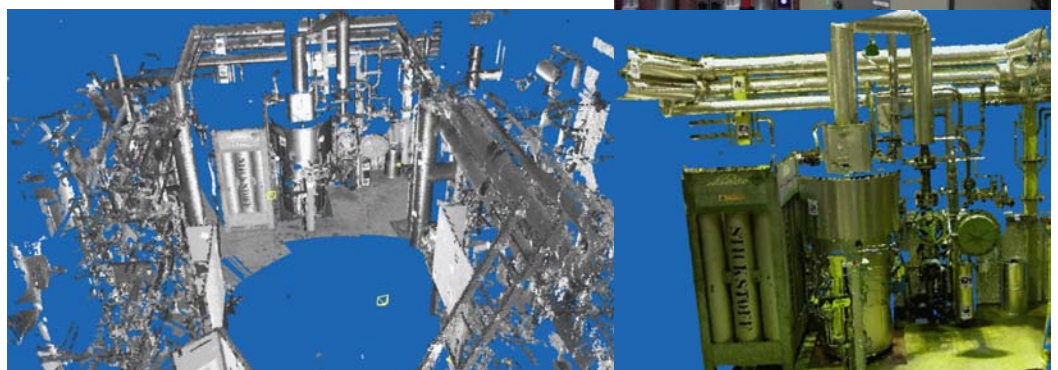
Reconstruction of industrial installations

- Make homogenous plan of existing factory, built in multiple stages
- Test fit of new planned installations
- Model production process digitally (e.g. liquid flow)



Factory Reconstruction

- Which type of scanner? Why?
- Problems:
- Automation: fitting of cylinders, planes
- Alternative methods:



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Forestry application

**Reconstruction of single trees
with precise stem cross sections**

Point cloud of different scans

Cross sections along the stem

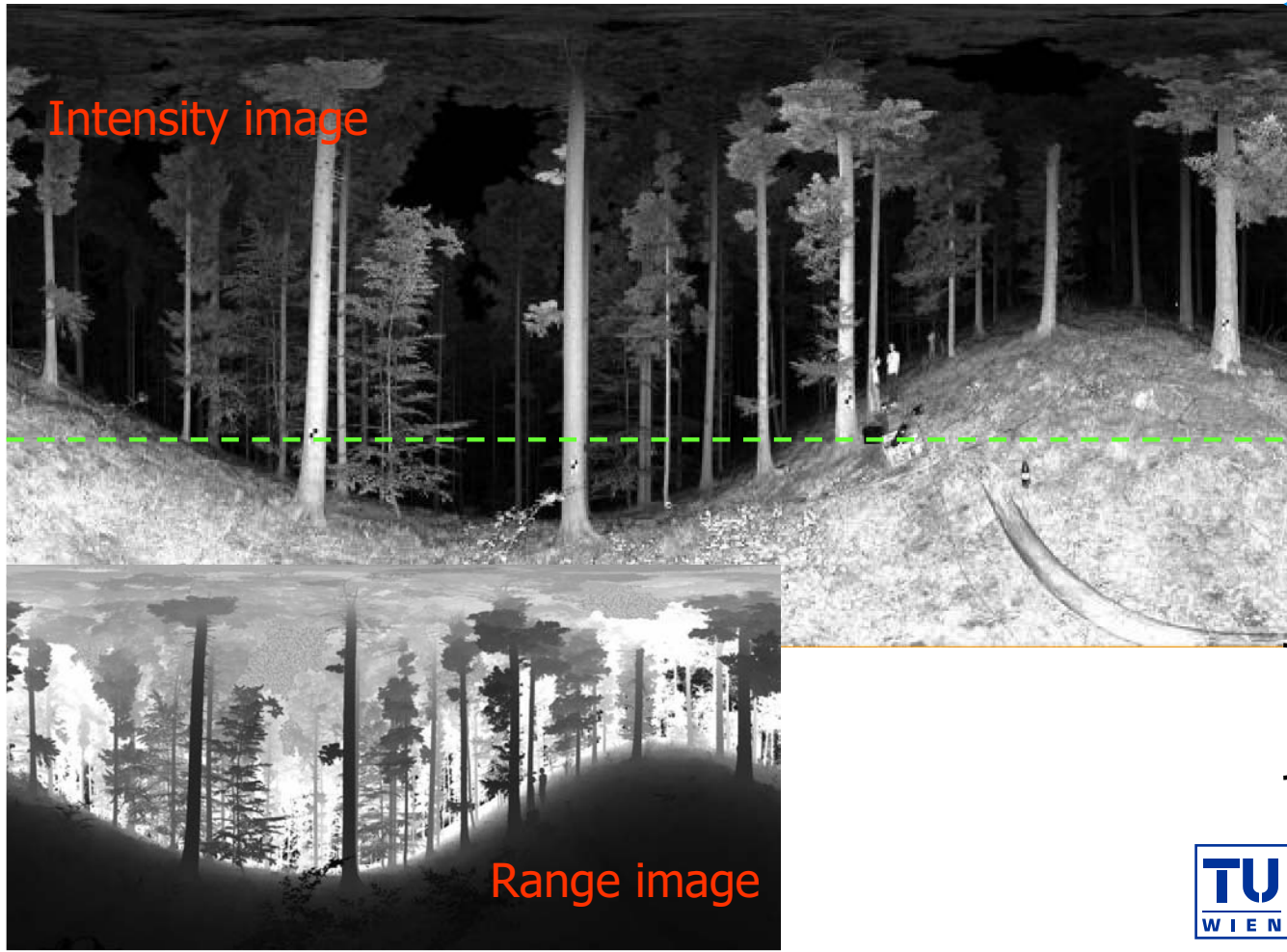
Next slide: data from one scan

Still in research state !



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360°



zenith

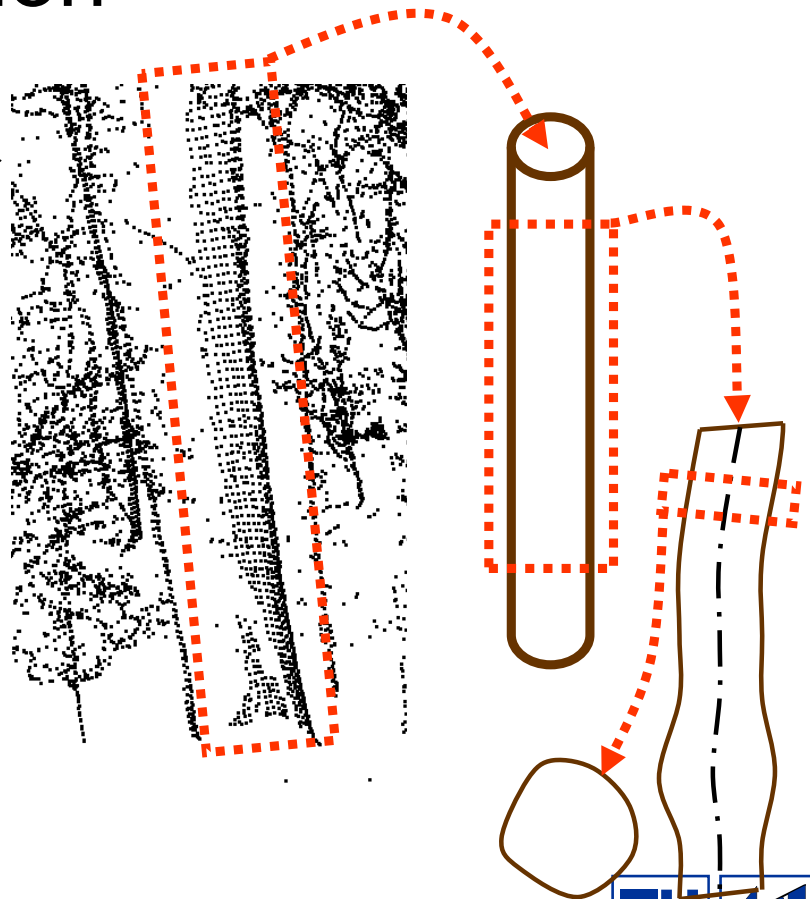
math. horizon

instrument base



Reconstruction steps

- Measurement ✓
- Registration ✓
- Coarse models
- Smooth branch models
- Cross sections



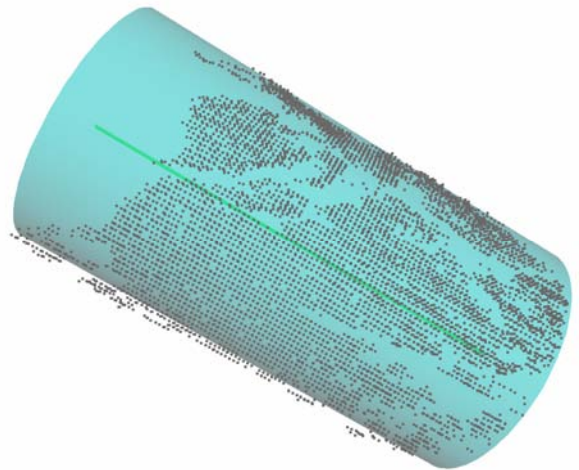
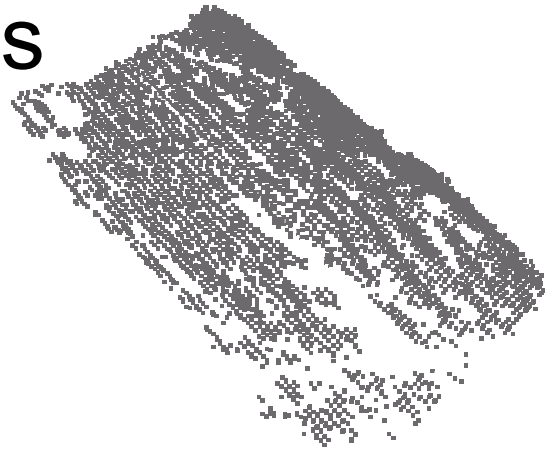
Coarse branch models

- Main parameters: radius, length
- Right circular cylinder

$$\|(\mathbf{Q}_i - \mathbf{P}) \times \mathbf{a}\| - r = 0$$

- parameters \mathbf{a} , r , \mathbf{P}
- observed points \mathbf{Q}_i
- Random measurement errors
Systematic deviation from model

$$\|(\mathbf{Q}_i - \mathbf{P}) \times \mathbf{a}\| - r = v_i$$



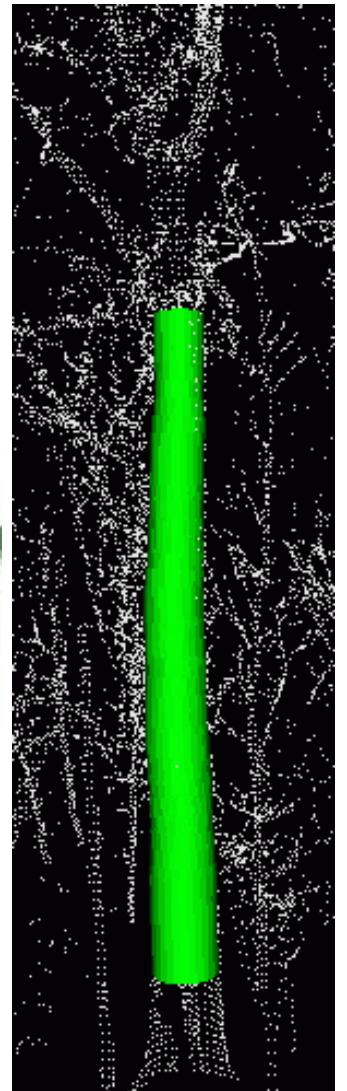
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Variation in radius and

- Real trees don't grow straight
- Real branches become thinner/thicker
→ Model only piecewise valid
→ Cylinder sequence
- Accuracy



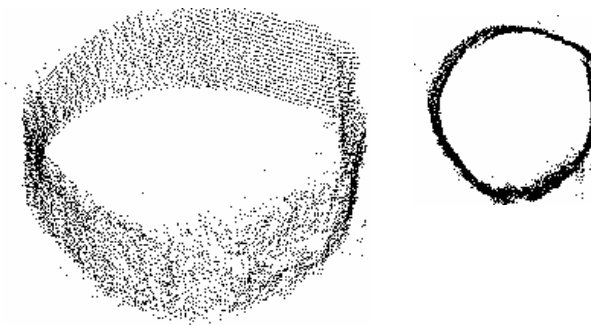
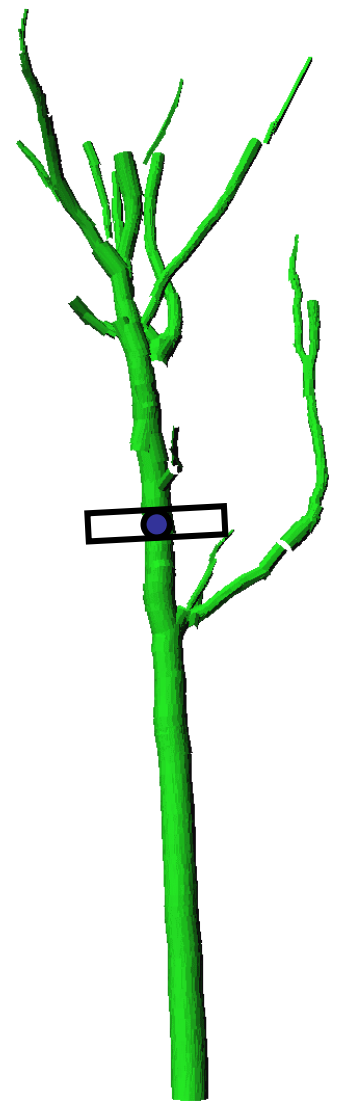
$$\sigma_0 = \sqrt{\sum_i v_i^2 / (n - 5)} \cong \pm 2\text{cm}$$



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Cross sections

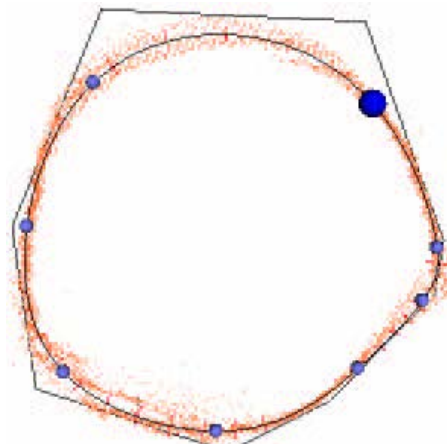
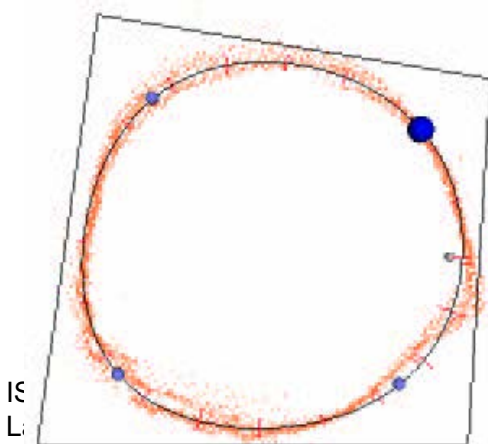
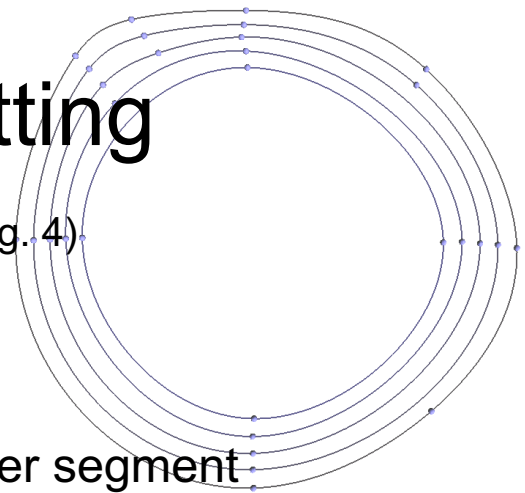
- Real branches don't have circular cross sections
 - select point on axis
 - cross section plane orthogonal to axis
 - select points in cross section plane
 - tolerance Δh e.g. 20cm
 - project points onto plane
 - ... 2D problem

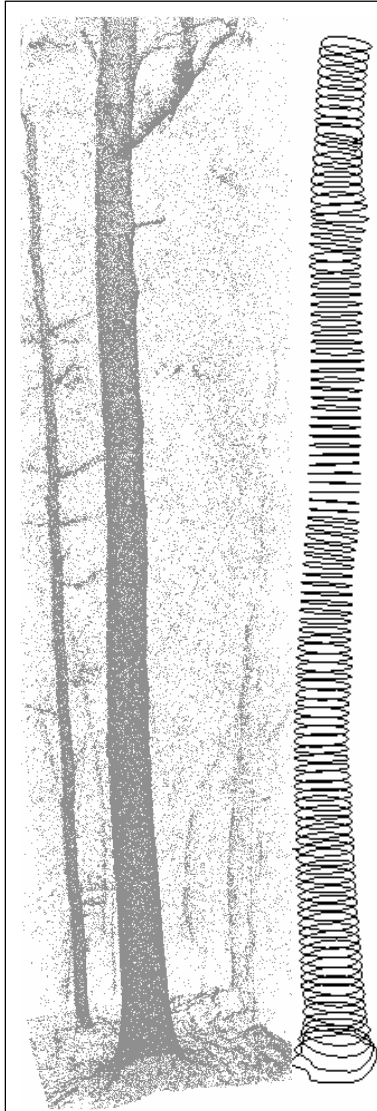


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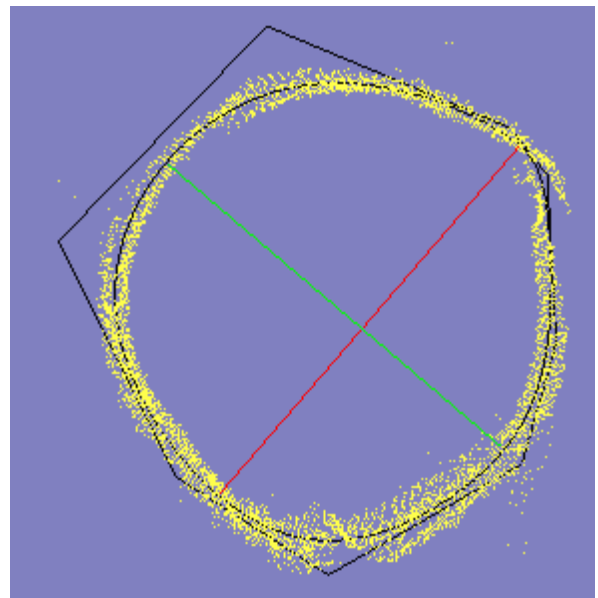
Spline curve fitting

- Choose number of segments (e.g. 4)
- Systematic deviations
- Insert vertices selectively
 - Measure systematic deviation δ_i per segment
 - Insert vertex at segment with highest δ_i

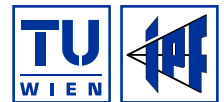




Usage



Relative measure
Minimum diameter / Maximum diameter
= wood quality
= economic revenue



Conclusions

Terrestrial laser scanning

- Is a method for the acquisition of points on surfaces (no edges, no corners)
- Featuring different systems with different performance



Conclusions

Terrestrial laser scanning is

- fast,
- accurate,
- a combination of photogrammetry, total stations and coordinate measurement machines,
- easy to use,
- and finally a method that is developing (commercially available since ~1990s).

It is becoming a standard method for surveying tasks, excluding: